# The Effect of Burnup on Reactivity for VVER-1000 with MOXGD and UGD Fuel Assemblies Using MCNPX Code

Heba K. Louis<sup>\*</sup>, Esmat Amin

Safety Engineering Department, Nuclear and Radiological Regulation Authority (NRRA), Cairo, Egypt

**Abstract** The neutronic calculations for power reactors are one of the most important steps for the safety of reactors. Performing calculations on benchmark problems related to neutronics calculations on the lattice and core levels is a preliminary step for the preparation of human building capabilities in neutronic calculations for power reactors. In present work the computational benchmarks of low enriched uranium (LEU) and (MOX) fuel assemblies for VVER-1000 have been calculated by the Monte Carlo code (version MCNPX 2.7). The aim of this work is toevaluate the accuracy of the Russian used codes and libraries against the MCNPX code and the most recent ENDF libraries. Five calculational states are performed; these states cover the operational states and cold conditions. The variations of k-inf and assembly average isotopic composition versus burnup are calculated. Several reactivity effects as <sup>135</sup>Xe and <sup>149</sup>Sm poisoning; Soluble boron effect; Fuel temperature (Doppler) effect; Total temperature effect also are performed. To ensure that our existing calculational method can accurately model VVER-1000 reactors with mixed-oxide (MOX) fuel, comparison is required. A comparison of the results was performed with the of Monte carol code MCU-REA and with the benchmark mean results, in most results excellent agreement was observed.

Keywords VVER-1000, Pressurized water reactor (PWR), Burnup, Reactivity effect and MCNPX code

## **1. Introduction**

VVER (Water-Water Energetic Reactor) is one of the most successful and influential branches of nuclear power plant development, and the technology is widely distributed throughout the world.

Several benchmark exercises have been proposed by an international Experts Group at the OECD/NEA with the intent to investigate the core physics behavior of a VVER-1000 reactor loaded with 2/3rd of (LEU) fuel assemblies and 1/3rd of (MOX) fuel assemblies [1].

In the VVER-100 Benchmark a total of six solutions were performed from five countries with each participant using different methods and data combinations. Two of the solutions are based on continuous energy Monte Carlo methods, while the remaining solutions are based on collision probability (or similar) methods. The submitted solutions covered several data libraries.

The goal of this work is to perform calculations of the VVER-1000 computational benchmarks with a more recent tool and libraries and make individual comparison with that used by the Russians.

The results for computational benchmarks of (LEU) and

(MOX) fuel assemblies by using the Monte Carlo code (version MCNPX 2.7.0) [2] with ENDF/B-VII.1 (ENDF71x) library [3] are presented in the next sections.

MCNPX is a general-purpose Monte Carlo N–Particle code that can be used for neutron, photon, electron, or coupled neutron/photon/electron transport, including the capability to calculate eigenvalues for critical systems. The code treats an arbitrary three-dimensional configuration of materials in geometric cells bounded by first- and second-degree surfaces and fourth-degree elliptical tori.

The present results are compared with the benchmark mean results and with the results of the RRC-KI, Russian Federation; they used the MCU Monte Carlo code MCU-REA code. MCU-REA is a general-purpose continuous energy Monte Carlo code for solving the neutron transport problems including the depletion ones. It is used with both pointwise and step function representations of cross sections. MCU data libraries are DLC/MCUDAT-2.1 based on ENDF/B-VI; JENDL-3.2; BROND.

#### **Benchmark model specification**

The benchmark model consists of two assembly types:

- Uniform LEU fuel assembly with 12 U/Gd rods (UGD variant).
- Profiled MOX fuel assembly with 12 U/Gd rods (MOXGD variant).

The VVER-1000 assemblies are hexagonal in design and consist of one central tube, 312 fuel pin locations (12 of which are U/Gd rods), and 18 guide tubes. The clad and

<sup>\*</sup> Corresponding author:

heba.louis@yahoo.com (Heba K. Louis)

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structural materials are composed of a Zr-Nb alloy.



Figure 1. The configuration of uniform LEU fuel assembly with 12 Gd BA rods



**Figure 2.** The configuration of profiled MOX fuel assembly with 12 Gd BA rods

The UGD variant is shown in Figure 1 and consists offuel rods with 3.7 wt. % enrichment. The 12 U/Gd pins have a  $^{235}$ U enrichment of 3.6 wt. % and a Gd<sub>2</sub>O<sub>3</sub> content of 4.0

wt. %. The MOXGD variant is shown in Figure 2 and contains fuel rods with three different plutonium loadings. The central region contains MOX pins with 4.2 wt. % fissile plutonium (consisting of 93 wt.  $\%^{239}$ Pu), two rings of fuel rods with 3.0 wt. % fissile plutonium, and anouter ring of fuel rods with 2.0 wt. % fissile plutonium. The 12 U/Gd rods are in the same locations as in the UGD variant configuration and have the same design.

The benchmark asks for depletion calculations to a burnup of 40 MWd/kgHM along with several branch calculations at five specific sets of reactor states S1 to S5. The requested state is presented in table 1.

Table 1.	Calculation	states
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State	Description	Fuel temp., K	Non-fuel temp., K	<sup>135</sup> Xe and <sup>149</sup> Sm
<b>S</b> 1	Operating poisoned state	1027	575	Eq.*
S2	Operating non-poisoned state	1027	575	0.0
<b>S</b> 3	Hot state	575	575	0.0
<b>S4</b>	Hot state without boron acid	575	575	0.0
<b>S</b> 5	Cold state	300	300	0.0

\*Eq. Indicates equilibrium 135-Xe and 149-Sm concentration

## **2. Calculation Procedures**

This paper describes the detailed results of a benchmark study investigating the physics of aVVER-1000 reactor using low-enriched uranium and MOX fuel. The calculations were performed with the MCNPX code (version MCNPX 2.7). The cross section data for all of the isotopes are taken from the ENDF/B-VII.1 (ENDF71x). For criticality calculation, a total of 1000 neutron cycle with100 non active cycle and 10<sup>6</sup> histories per generation were used.

In the present paper, the calculations are performed for different states as following:

• For S1 state (operating poisoned state), burnup calculation has been performed with a power density of 108 MWt/m<sup>3</sup> up to a burnup of 40 MWD/kgHM with 21 burnup steps (1 MWd/kgHM in the interval 0 -15 MWd/kgHM and 5 MWd/kgHM in the interval 15-40 MWd/kgHM)). The present calculations for this state included:

- The variation of  $k_{\text{inf}}$  with burnup for UGD variant and MOXGD variant assemblies
- Averaged concentrations of the fuel assembly for <sup>235</sup>U, <sup>236</sup>U, <sup>238</sup>U, <sup>238</sup>Pu, <sup>239</sup>Pu, <sup>240</sup>Pu, <sup>241</sup>Pu, <sup>242</sup>Pu, <sup>135</sup>Xe, <sup>149</sup>Sm, <sup>155</sup>Gd and <sup>157</sup>Gd.

• Several reactivity effects at burnup levels 0, 20, 40 MWd/kgHMhave been determined based on the  $k_{inf}$  values corresponding to the reactor states as follow:

 <sup>135</sup>Xe and <sup>149</sup>Sm poisoning effect on reactivity have been determined based on the k<sub>inf</sub> values corresponding to the reactor states S1 (operating poisoned state) and S2 (operating non-poisoned state);

- soluble boron effect on reactivity for a boron change of 600 ppm has been determined based on the k<sub>inf</sub> values corresponding to the reactor states S3 (isothermal hot state with boron) and S4 (isothermal hot state without boron);
- Fuel temperature (Doppler) effect on reactivity of assemblies for a fuel temperature change from 575 to 1027 K has been determined based on the  $k_{inf}$  values corresponding to the reactor states S2 (state with  $T_{fuel} =$  1027 K) and S3 (state with  $T_{fuel} =$  575 K) have been used; and
- Total temperature effect on reactivity of assemblies for a temperature change from 300 K to 575 K has been determined based on the  $k_{inf}$  values corresponding to the reactor states S4 (hot state T = 575 K) and S5 (cold state with T = 300 K).

## 3. Results and Discussion

As mentioned previously, the calculations for the five reactor states have been performed using MCNPX code with ENDF/B-VII.1 (ENDF71x) library. The results are presented in the following:

#### 3.1. The Variation of k-inf with Burnup

The results of infinite multiplication factors for UGD variant fuel assembly and MOX fuel assembly with respect to burnup for the operating poisoned state (S1) is shown in Figure 4.

Figure 4 shows the comparison of the MCNPX results with both the benchmark's participants mean results and MCU results.

As shown in figure 4 we can see that for UGD variant assembly, as the burnup increases the k-inf initially increases due to the rapid burn out of the Gd isotopes and the buildup of Pu-239 and then, decreases while for MOXGD variant assembly the burn up of Pu-239 is not compensated by the butnup of gadolinium isotopes and then, decreases faster with almost the complete burnup of gadolinium.

The deviation of the MCNPX results from the mean benchmark results and the Russian MCU code are small and amounts to a maximum of 0.565, 0.679 for UGD variant and 0.650, 0.979 for MOXGD variant.



Figure 4. Variation of K-inf with respect to burnup for UGD variant and MOXGD variant assemblies



Figure 5. Assembly average U-235 composition vs. burnup



Figure 6. Assembly average U-236 composition vs. burnup







Figure 8. Assembly average PU-239 composition vs. burnup







Figure 10. Assembly average PU-241 composition vs. burnup



Figure 11. Assembly average PU-242 composition vs. burnup



Figure 12. Assembly average Xe-135 composition vs. burnup



Figure 13. Assembly average Sm-149 composition vs. burnup



Figure 14. Assembly average Gd-155 composition vs. burnup



Figure 15. Assembly average Gd-157 composition vs. burnup

#### 3.2. Assembly Average Isotopic Composition verse to Burnup

The changes in isotopic composition with respect to burnup for various fuel nuclides (<sup>235</sup>U, <sup>236</sup>U, <sup>238</sup>U, <sup>238</sup>Pu, <sup>239</sup>Pu, <sup>240</sup>Pu, <sup>241</sup>Pu, <sup>242</sup>Pu, <sup>135</sup>Xe, <sup>149</sup>Sm, <sup>155</sup>Gd and <sup>157</sup>Gd) are calculated for both UGD and MOX fuel assembly and are presented in figures 5- 15 respectively.

From figures 5-15 we can see that, at low burnup there is an excellent agreement with benchmark mean results and with MCU results for all isotopes in UGD and MOXGD assemblies. While at high burnup for some isotopes the discrepancies are somewhat increased but in most figures good agreement was observed. The depletion rate of <sup>235</sup>U isotope for UGD assembly is larger than that for MOXGD assembly. The buildup rate of <sup>236</sup>U isotope is very large in UGD assembly than in MOXGD assembly.

For both UGD and MOXGD assemblies the <sup>157</sup>Gd depletes more rapidly than <sup>155</sup>Gd because the absorption cross section of <sup>157</sup>Gd is higher than the absorption cross section of <sup>155</sup>Gd. Also, both of the gadolinium isotopes <sup>155</sup>Gd and <sup>157</sup>Gd burn rapidly in UGD assembly than in MOXGD assembly.

#### 3.3. k-inf Effects Results for States S1-S5

The burnup calculation has been performed at burnup points 0, 20, 40 MWd/kgHM for states S1-S5. The variations of  $k_{inf}$  states (S1, S2, S3, S4, and S5) with respect to burnup (MWD/KgHM) for UGD and MOXGD assemblies are shown in tables 2 and 3 respectively.

Several reactivity effects at burnup points 0, 20, 40 MWd/kgHM have been determined based on the  $k_{inf}$  values corresponding to the reactor states as mentioned previously in calculation procedure section. The results of reactivity effects are compared with MCU result and benchmark mean results and presented in tables 4 and 5 for both UGD and MOXGD assemblies respectively. Also the MCNPX results deviations from benchmark mean results and from MCU code results are presented in tables 6 and 7.

Table 2. UGD variant.  $k_{\text{inf}}$  states S1- S5 with respect to burnup (MWD/KgHM)

Burnup	S1	<b>S2</b>	<b>S</b> 3	S4	<b>S</b> 5
	MCNPX code				
0	1.134	1.171	1.183	1.252	1.322
20	1.047	1.082	1.093	1.144	1.203
40	0.915	0.941	0.960	1.004	1.067
	MCU code				
0	1.1353	1.1779	1.1899	1.2499	1.3197
20	1.0403	1.0809	1.0950	1.1496	1.2192
40	0.9091	0.9433	0.9562	1.0063	1.0632
Benchmark Mean					
0	1.1350	1.1754	1.1891	1.2489	1.3175
20	1.0411	1.0807	1.0959	1.1507	1.2179
40	0.9065	0.9394	0.9534	1.0025	1.0558

From tables 2 and 3 we can see very good agreements for all MCNPX results with both of MCU code and Benchmark Mean results.

Burnup	<b>S1</b>	S2	<b>S</b> 3	S4	<b>S</b> 5	
		MCNP	X code			
0	1.159	1.194	1.213	1.254	1.331	
20	1.018	1.048	1.062	1.098	1.174	
40	0.904	0.942	0.947	0.998	1.054	
	MCU code					
0	1.1551	1.1873	1.2045	1.2384	1.3176	
20	1.0126	1.0482	1.0626	1.1005	1.1739	
40	0.9075	0.9390	0.9529	0.9933	1.0522	
Benchmark Mean						
0	1.1566	1.1899	1.2074	1.2422	1.3209	
20	1.0160	1.0504	1.0659	1.1042	1.1746	
40	0.9015	0.9323	0.9464	0.9862	1.0403	

Table 3. MOXGD variant  $.k_{\rm inf}$  states S1-S5 with respect to burnup (MWD/KgHM)

 Table 4.
 UGD Variant. Reactivity effects, 100\*(k<sub>init</sub>-k<sub>final</sub>)

Burnup	MCNPX	MCU	B. Mean		
<sup>135</sup> X	Ke and <sup>149</sup> Sm poison	ing effect, [(K <sub>S1</sub>	-K <sub>S2</sub> ) *100]		
0	-3.71	-4.26	-4.04		
20	-3.44	-4.06	-3.96		
40	-2.66	-3.42	-3.29		
Fuel	temperature (Dopp	oler) effect, [(K <sub>s</sub>	<sub>2</sub> -K <sub>83</sub> ) *100]		
0	-1.25	-1.20	-1.37		
20	-1.19	-1.41	-1.52		
40	-1.89	-1.29	-1.40		
	Soluble boron effect, [(K <sub>S3</sub> -K <sub>S4</sub> ) *100]				
0	-6.85	-6.00	-5.98		
20	-5.11	-5.46	-5.48		
40	-4.39	-5.01	-4.91		
Total temperature effect, [(K <sub>S4</sub> -K <sub>S5</sub> ) *100]					
0	-7.08	-6.98	-6.86		
20	-5.90	-6.96	-6.72		
40	-6.30	-5.69	-5.33		

#### From Tables 4 and 5 we can see that:

- The reactivity effect of <sup>135</sup>Xe and <sup>149</sup>Sm on reactivity is less negative in MOXGD assembly than in UGD this because of the harder neutron spectrum in the MOXGD assembly. The calculated reactivity effect of xenon and samarium by MCNPX code are close to the benchmark mean value and with MCU code.
- The reactivity effect of fuel temperature on reactivity (Doppler Effect) is more negative in MOXGD assembly than in UGD. The calculated reactivity effect of fuel temperature by MCNPX code is close to the benchmark mean value and with MCU code.
- The reactivity effect of soluble boron on reactivity is less negative in MOXGD assembly than in UGD. The

calculated reactivity effect of boron by MCNPX code is close to the benchmark mean value and with MCU code.

- Total temperature effect on reactivity is more negative in MOXGD assembly than in UGD, this due to harder neutron spectrum in MOXGD assembly. The calculated reactivity effect of total temperature by MCNPX code is close to the benchmark mean value and with MCU code.

Burnup	MCNPX	MCU	B. Mean		
<sup>135</sup> X	<sup>135</sup> Xe and <sup>149</sup> Sm poisoning effect, [(K <sub>S1</sub> -K <sub>S2</sub> ) *100]				
0	-3.52	-3.22	-3.33		
20	-2.93	-3.56	-3.44		
40	-3.76	-3.15	-3.08		
Fuel	Fuel temperature (Doppler) effect, [(K <sub>S2</sub> -K <sub>S3</sub> ) *100]				
0	-1.90	-1.72	-1.75		
20	-1.40	-1.44	-1.55		
40	-0.55	-1.39	-1.41		
	Soluble boron effect, [(K <sub>S3</sub> -K <sub>S4</sub> ) *100]				
0	-4.06	-3.39	-3.48		
20	-3.64	-3.79	-3.83		
40	-5.10	-4.04	-3.98		
Total temperature effect, [(K <sub>S4</sub> -K <sub>S5</sub> ) *100]					
0	-7.76	-7.92	-7.87		
20	-7.63	-7.34	-7.04		
40	-5.58	-5.89	-5.41		

Table 5. MOXGD Variant. Reactivity effects, 100\*(kinit-kfinal)

 Table 6.
 UGD Variant. MCNPX Relative Deviation from MCU and Mean

100%*(MCNPX-MCU)/MCU	100%*(MCNPX-Mean)/Mean			
For <sup>135</sup> Xe and <sup>149</sup> Sm poisoning effect				
-0.13	-0.08			
-0.15	-0.13			
-0.22	-0.19			
For Fuel temperature (Doppler) effect				
0.04	-0.09			
-0.16	-0.22			
0.47	0.35			
For Soluble boron effect				
0.14	0.14			
-0.06	-0.07			
-0.12	-0.11			
For Total temperature effect				
0.01	0.03			
-0.15	-0.12			
0.11	0.18			

100%\*(MCNPX-MCU)/MCU 100%\*(MCNPX-Mean)/Mean For <sup>135</sup>Xe and <sup>149</sup>Sm poisoning effect 0.09 0.06 -0.18 -0.15 0.19 0.22 For Fuel temperature (Doppler) effect 0.10 0.08 -0.03 -0.10 -0.61 -0.61 For Soluble boron effect 0.20 0.17 -0.04 -0.05 0.26 0.28 For Total temperature effect -0.02 -0.01 0.04 0.08 -0.05 0.03

 Table 7.
 MOXGD Variant. MCNPX Relative Deviation from MCU and Mean

#### From Tables 6 and 7 we can see that:

- For The reactivity effect of <sup>135</sup>Xe and <sup>149</sup>Sm, the maximum absolute deviations from benchmark mean values and MCU code are 0.19 and 0.22 respectively for UGD assembly. While for MOXGD assembly the maximum absolute deviations from benchmark mean values and MCU code are 0.22 and 0.19 respectively.
- For Doppler Effect the maximum absolute deviations from benchmark mean values and MCU code are 0.35 and 0.47 respectively for UGD assembly. While for MOXGD assembly the maximum absolute deviations from benchmark mean values and MCU code are 0.61 and 0.61 respectively.
- For Soluble boron effect, the maximum absolute deviations from benchmark mean values and MCU code are 0.14 and 0.14 respectively for UGD assembly. While for MOXGD assembly the maximum absolute deviations from benchmark mean values and MCU code are 0.28 and 0.26 respectively.
- For total temperature effect, the maximum absolute deviations from benchmark mean values and MCU code are 0.18 and 0.15 respectively for UGD assembly. While for MOXGD assembly the maximum absolute deviations from benchmark mean values and MCU code are 0.08 and 0.05 respectively.

The results of comparison of the reactivity effects show very good agreement. Discrepancies for reactivity effects are approximately the same both for UGD and MOXGD variants and are somewhat increased at high burnup.

## 4. Conclusions

In the present paper the computational benchmarks of UGD and MOXGD variants fuel assemblies for VVER-1000 have been calculated by the Monte Carlo code (version MCNPX 2.7). The obtained results of the K-inf and the variation of fission products concentrations with respect to burnup and several reactivity effects were performed and have been compared with those of Monte carol results by MCU-REA code and with the benchmark mean results of other codes presented in the benchmark. The MCNPX results of the k<sub>inf</sub> values versus burnup show generally good agreement.

Assembly average isotopic composition verse to burnup are calculated, at low burnup there is an excellent agreement with benchmark mean results and with MCU results for all isotopes in UGD and MOXGD assemblies. While at high burnup for some isotopes the discrepancies are somewhat increased but in most figures good agreement was observed.

The results of comparison of the reactivity effects show very good agreement. Discrepancies for reactivity effects are approximately the same both for UGD and MOXGD variants and are somewhat increased at high burnup.

In most cases very good agreement was observed. Slightly deviations was observed due to we used ENDEF-VII nuclear data library while the codes in the benchmark used other nuclear data libraries (ENDF/B-VI, JEF-2.2 and MCUDAT-2.1).

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