

Back Analysis of Slope Failure Using Finite Element with Point Estimate Method (FEM-PEM)

Soon Min Ng^{*}, Mohd Ashraf Mohamad Ismail, Ismail Abustan

School of Civil Engineering, Universiti Sains Malaysia (USM), Engineering Campus, Pulau Pinang, Malaysia

Abstract This paper investigates the slope failure in Precinct 9, Putrajaya, Malaysia by using numerical back analysis method. The catastrophic slope failure was triggered by a cumulative rainfall of 210 mm that occurred 2 days before the occurrence of slope failure. Site investigation that includes borehole sampling was immediately conducted to obtain representative information for the study area. The slope can be divided into 3 layers namely gravelly silt, silt and bedrock. Due to the uncertainty about the actual cause of failure initiation, back analyses have been performed via finite element shear strength reduction method for considering various probable mechanisms. In order to deal with the uncertainty and variability of the soil parameters, the Point Estimate Method (PEM) approach that assumed a normal and uncorrelated distribution was adopted in this study. Analysis results show that the slope failure is mainly influenced by the shear strength of the silt layer where the cohesion and friction angle at failure were 11 kPa and 20° respectively. Besides, the modeled circular slip surface also agrees well with the observed one.

Keywords Back analysis, Slope failure, Shear strength reduction, Point estimate method

1. Introduction

The analysis carried out to identify the cause of slope failure is known as back analysis. It can be utilized to determine the shear strength parameters, pore water pressure and other conditions at the time of failure. Generally, back analysis is an effective approach to provide an insight into the underlying failure mechanism and improve the understanding regarding the factors controlling the stability of slopes. One of the advantages of back analysis is it can account for important factors that may not be well represented in laboratory and in-situ tests such as the presence of cracks and pre-existing shear planes within the soil mass [1]. Besides, the scale for back analysis is also much larger compared to the materials that are in in-situ state [2]. However, there are also some uncertainties in back analysis approach that must be considered. For examples, mechanism of progressive slope failure, information of pore water pressure and the exact slip surface location and geometry [3].

Two methods that can be used to perform back analysis are deterministic and probabilistic method. Deterministic method determines a unique set of parameter such as c and ϕ by considering the factor of safety equals to unity [4]. However, in order to deal with the uncertainties in back

analysis, probabilistic method offers a better approach to analyze a multiple sets of parameters simultaneously [5]. The outcomes are numerous combinations of parameters that result in slope failure. Nevertheless, the results of probabilistic method are realistic if the input parameters were correctly statistically characterized [6].

In this paper, a systematic approach of back analysis is proposed using the probabilistic method. The objective of this study is to identify a range of possibilities that cause slope failure from the available information and to determine the suitable parameters that can be used for designing remedial works. The reliability of this approach is demonstrated by applying it to a case study of slope failure in Putrajaya, Malaysia.

2. Project Background

Putrajaya is the third federal territory of Malaysia that serves as the federal administrative centre for the country. It has approximately 49 km² of land and was developed due to the congestion and overcrowding in Kuala Lumpur areas. A slope failure that involved 20 m height of man-made slope about 45° occurred on 22nd March 2007 at Precinct 9, Putrajaya. 23 vehicles were buried by the debris and 1000 residents were forced to vacate from their 15 stories apartment which is located 10 m from the failure zone. Prior to the slope failure that occurred at 4.30am, it had been raining heavily in Putrajaya since the evening of 20th March 2007 until the early morning of 22nd.

^{*} Corresponding author:

soonmin1612@hotmail.com (Soon Min Ng)

Published online at <http://journal.sapub.org/jce>

Copyright © 2014 Scientific & Academic Publishing. All Rights Reserved

The slope failure occurred on the western side of a 50m high hill with a 36 million water tank constructed on the crest. The study area is underlain by graphitic quartz mica schist from Kajang Formation. Based on historical site investigation, the rocks in this area consist of interbedded sandstone, shale and actinolite schist [7]. Fig. 1 shows the location of the slope failure in Precint 9, Putrajaya.

3. Site Investigation

The study commenced with desk study where data collection for hydrological, geological and topographical data were conducted. Rainfall data recorded by a rain gauge station located near to the study area show a high intensity of rainfall of 140mm and 60mm on 20th and 21st March 2007. The rainfall intensity on 22nd March 2007 which is the day of slope failure recorded only 10mm.

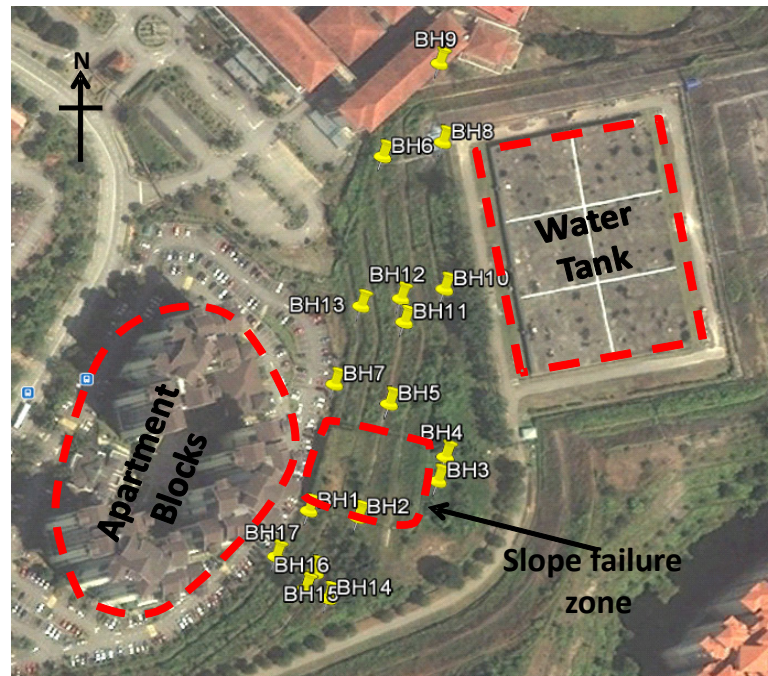


Figure 1. Location of slope failure and boreholes in Precint 9, Putrajaya

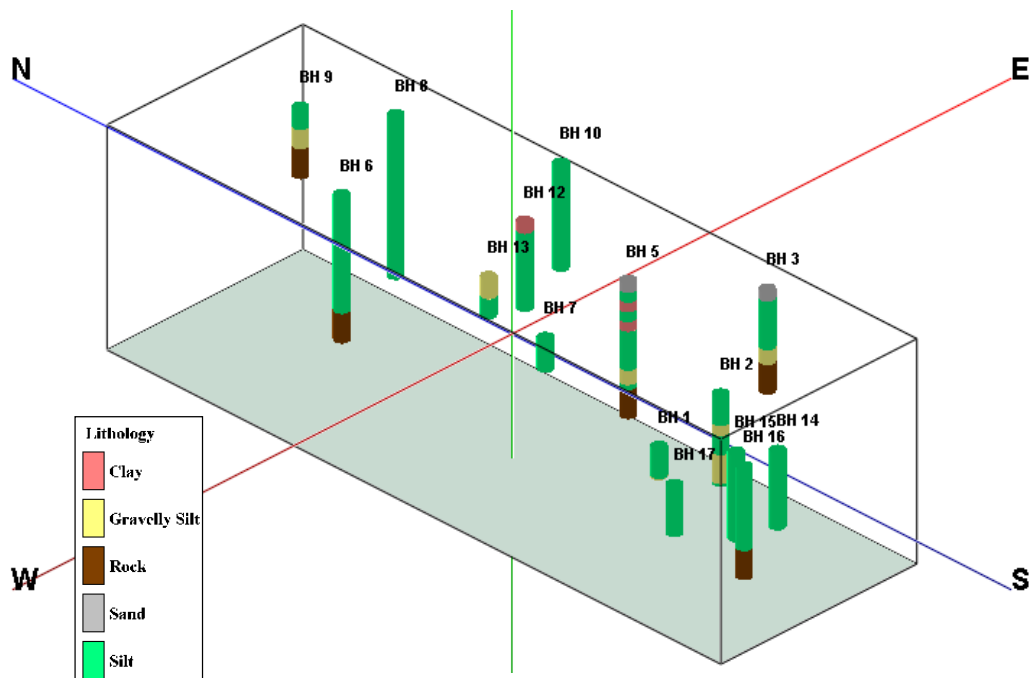


Figure 2. 3-dimensional multi boreholes log

A total of 17 boreholes drilling were carried out using rotary wash boring method immediately after the slope failure and their location are as shown in Fig. 1. The purpose of this borehole drilling was to determine the subsurface characteristics of the study area such as depth, groundwater level, lithology, and standard penetration (SPT) value and to collect soil sample for laboratory testing. Standard penetration test (SPT) was conducted in accordance to BS1377: Part 9: 1990 using a self tripping hammer of 63.5kg [8]. Initially, the tests were carried out at 1m interval from the ground surface to a depth of 6m and subsequently at every 1.5m intervals or when change of strata was encountered.

Soil samples were collected in the form of disturbed and undisturbed samples to determine the soil parameters input for back analysis. Rock coring in accordance to BS5930: 1999 was also carried out when a rock layer is encountered [9]. The core recovery ratio (CRR) and rock quality designation (RQD) was recorded for each core run. Groundwater level in each borehole was measured using electric dipmeter when the drilling is in progress and after the completion of the boreholes. The borehole data were then utilized to develop a 3-dimensional multi boreholes logs model as shown in Fig. 2. This 3D model is able to show the types of soil that present in the study area and enable the development of conceptual model that will be used for back analysis.

4. Results and Discussions

Generally, the slope consists of 3 layers namely silt, gravelly silt and bedrock. A conceptual model for the slope was developed as shown in Fig. 3. Point estimate method (PEM) developed by Rosenblueth (1975) [10] was used in this study to deal with the probabilistic inputs in slope stability analysis. The principle of PEM is to compute solutions at various estimation points and to combine them

with proper weighting in order to get an approximation of the distribution of the output variables. The fundamental assumption to use PEM is all random variables are normally distributed. In this study, the numerical computation for PEM will be solved together with finite element shear strength reduction analysis using *Phase2* software [11].

The input parameters values obtained from laboratory testing that will be used for the analysis are as shown in Table 1. The random variables chosen for probabilistic analysis are cohesion and friction angle for both silt and gravelly silt soil that result in 16 sets of combination. Table 2 shows the factor of safety (FOS) computed with different combination of random variables using PEM method. The results showed that the FOS at unity was produced by cohesion and friction angle of silt soil with the value 11 kPa and 20° respectively. This indicates that the stability of slope is mostly influenced by the silt layer and the slip surface produced match the observed one as shown in Fig. 4.

Table 1. Input parameters for stability analysis

Material Parameter	Silt	Gravelly Silt
Soil constitutive model	Mohr Coulomb	
Unit weight [kN/m ³]	18.67	17.79
Cohesion [k.Pa]	14	36
Friction angle [°]	23	18
Hydraulic conductivity [m/s]	1.17×10^{-10}	2.42×10^{-10}

To verify the results of probabilistic PEM method, a sensitivity analysis was carried out using limit equilibrium (LEM) with Monte Carlo probabilistic method and the results is plotted in Fig. 5. The sensitivity plot agrees well with the results of PEM where the cohesion and friction angle of 10.36 kPa and 19.09° will result in slope failure. The sensitivity plot also shows that the FOS is less sensitive to gravelly silt layer. From this back analysis, remedial work can be designed based on the shear strength parameters of the silt soil computed at the time of failure.

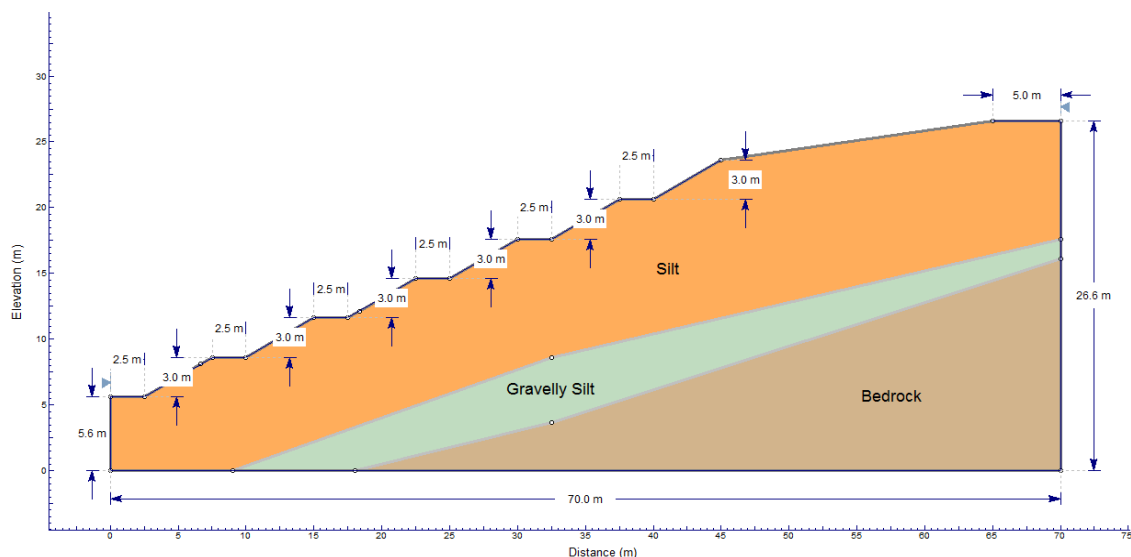
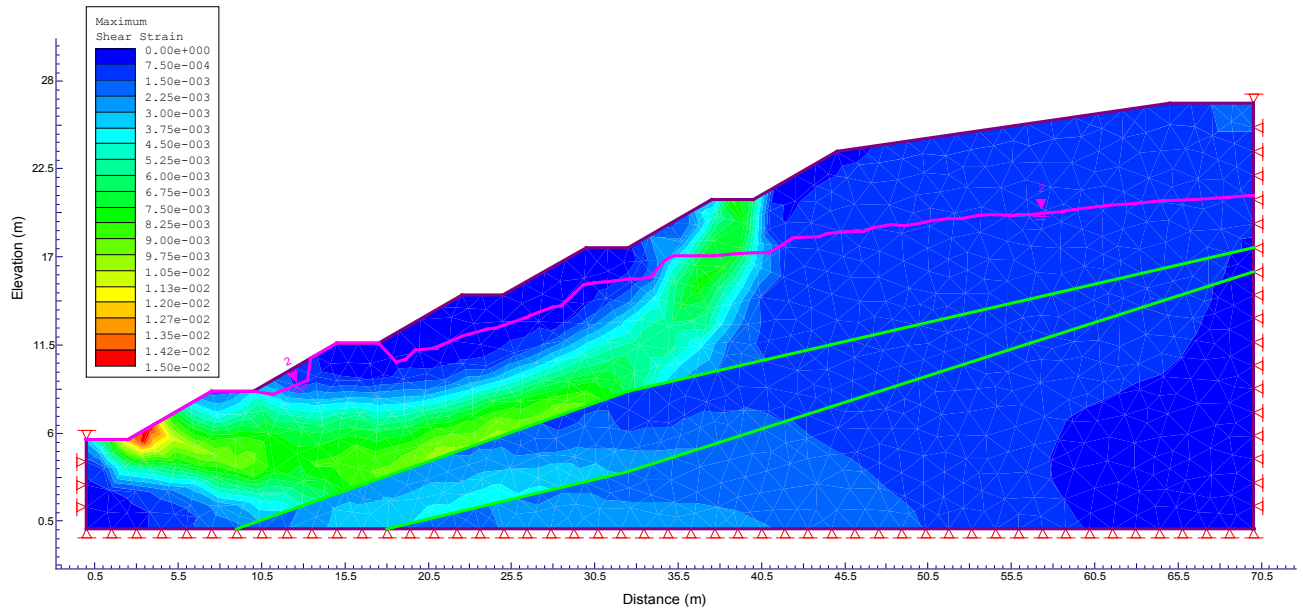
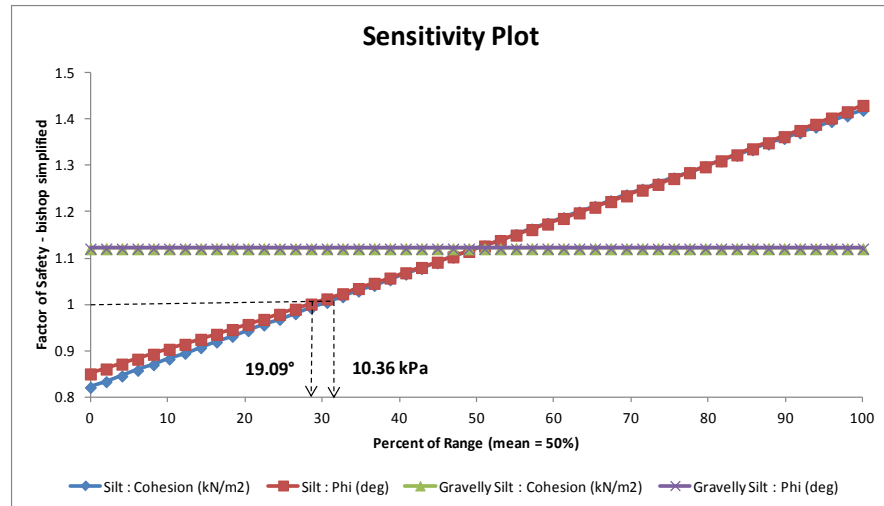


Figure 3. Conceptual model for the slope

Table 2. Factor of safety (FOS) with different combination of random variables

Combination No.	Gravelly silt		Silt		Factor of Safety
	Friction Angle (°)	Cohesion (kPa)	Friction Angle (°)	Cohesion (kPa)	
1	21	39	26	17	1.53
2	15	39	26	17	1.53
3	21	33	26	17	1.54
4	15	33	26	17	1.5
5	21	39	20	17	1.28
6	15	39	20	17	1.29
7	21	33	20	17	1.29
8	15	33	20	17	1.31
9	21	39	26	11	1.28
10	15	39	26	11	1.3
11	21	33	26	11	1.29
12	15	33	26	11	1.31
13	21	39	20	11	1.06
14	15	39	20	11	1.06
15	21	33	20	11	1.06
16	15	33	20	11	1.06

**Figure 4.** Slip surface computed with finite element shear strength reduction method**Figure 5.** Sensitivity plot via LEM-Monte Carlo probabilistic method

5. Conclusions

Based on the back analysis carried out, the stability of the slope in Precinct 9, Putrajaya is generally influenced by the silt layer. The shear strength parameters computed at the verge of slope failure are 11 kPa and 20° for cohesion and friction angle respectively. These threshold values can be utilized for remedial works such as installation of slope stabilization measures or designing a new slope under similar geotechnical conditions. This study also shows that the PEM approach is able to deal with the uncertainty and variability in FEM analysis. However, in order to maximize the use of PEM-FEM approach in back analysis, information should be combined from all possible sources such as laboratory testing, field instrumentation, and experience.

ACKNOWLEDGEMENTS

The authors would like to express their appreciation to Universiti Sains Malaysia Research University (RU) Grant (1001/PAWAM/814192) for the financial support to carry out this research. In addition, the authors would also like to acknowledge Putrajaya Corporation and Kumpulan Ikram for the permission to carry out this research at the site and the cooperation given to make this research a success.

REFERENCES

- [1] Duncan, J. M., and Timothy, D. S. "Soil strengths from back analysis of slope failures." *Stability and Performance of Slopes and Embankments II*. ASCE, (1993).
- [2] Gilbert, R. B., Stephen, G. W., and Eric, L. "Uncertainty in back analysis of slopes: Kettleman Hills case history." *Journal of Geotechnical and Geoenvironmental Engineering* 124.12 (1998): 1167-1176.
- [3] Deschamps, R., and Greg, Y. "Limitations in the back-analysis of strength from failures." *Journal of geotechnical and geoenvironmental engineering* 132.4 (2006): 532-536.
- [4] Jiang, Jing-Cai, and Takuo Yamagami. "A new back analysis of strength parameters from single slips." *Computers and Geotechnics* 35.2 (2008): 286-291.
- [5] Zhang, J., Wilson H. Tang, and L. M. Zhang. "Efficient probabilistic back-analysis of slope stability model parameters." *Journal of geotechnical and geoenvironmental engineering* 136.1 (2009): 99-109.
- [6] Wang, L., Hwang, J. H., Luo, Z., Juang, C. H., & Xiao, J. "Probabilistic back analysis of slope failure—A case study in Taiwan." *Computers and Geotechnics* 51 (2013): 12-23.
- [7] Ahmed, J., Ghazali, M. A., Mukhlisin, M., Alias, M. N. and Taha, M. R.. Effectiveness of horizontal drains in improving slope stability: a case study of landslide event in Putrajaya Precinct 9, Malaysia. *Unsaturated Soils: Theory and Practice* (2011). Jatisankasa, Sawangsuriya, Sorolump and Mairaing. Kasetsart University, Thailand. 753-758p.
- [8] British Standard. *Methods for test for soils for civil engineering purposes – 1377 Part 9: In-situ Tests*. (1990).
- [9] British Standard. *Code of practice for site investigations – 5930*. (1999).
- [10] Rosenblueth, E. "Point estimates for probability moments." *Proceedings of the National Academy of Sciences* 72.10 (1975): 3812-3814.
- [11] Rocscience Inc. *Phase2 v7.0 – Two-dimensional finite element slope stability analysis*. (2008).