

Prognosticating the Production Performance of Saturated Gas Drive Reservoir: A Theoretical Perspective

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Abstract Saturated gas drive reservoirs are characterized by rapid and continuous decline of reservoir pressure. The resultant effect of this phenomenon is the early decline of reservoir performance at the primary stage of the life of the reservoir. The recovery of hydrocarbon from this type of reservoir through the conventional lifting (spontaneous production) is inefficient and uneconomic due to its least recovery efficiency leading to significant amount of residual oil. The Muskat model was used to analyze solution-gas drive reservoir and predict its primary oil recovery. The inflow performance of the reservoir was analyzed through the Fetkovich model. Outflow performance of various tubing sizes such as 2", 2.5", 3" and 4" was analyzed. The future performance of reservoir is forecasted in the three stages: the first one is to predict cumulative hydrocarbon production as a function of declining reservoir pressure, the second stage is time-production phase, and the third stage of prediction is the time-pressure phase. From the inflow performance relationship IPR analysis the maximum inflow rate obtainable is 1710bpd with outflow rate of 1200bpd. The flow capacity near the abandonment reaches 77bpd at about 15925days with cumulative oil produced as 7M Mstb.

Keywords Solution Gas Drive, Recovery, Inflow Performance, Outflow Performance, Tubing String

1. Introduction

Saturated gas drive is one of the depletion drive reservoirs in which the principal drive mechanism is the expansion of the oil and its originally dissolved gas as well as the associated pore space. The increase in fluid volumes during the process is equivalent to the production. As pressure is reduced rapidly and continuously in this type of reservoir remarked by [1], oil expands due to compressibility and eventually gas comes out of solution from the oil as the bubble point pressure of the fluid is reached. The expanding gas provides the force to drive the oil hence the term solution gas drive. It is sometimes called dissolved gas drive [2].

In solution gas drive reservoirs the initial condition is where the reservoir is under-saturated, i.e. above the bubble point. Production of fluids down to the bubble point is as a result of effective compressibility of the system. This part of the depletion drive may be termed compressibility drive. The low compressibility causes rapid pressure decline in this period and resulting low recovery. Below the bubble point, the expansion of the connate water and the rock

compressibility are negligible hence as the oil phase contracts owing to the release of gas from solution, oil production therefore occurs as a result of expansion of the gas phase.

When the gas saturation reaches the critical value, the free gas begins to flow. At fairly low gas saturations, the gas mobility, k_g/u_g , becomes large and the oil mobility, k_o/u_o , is small, resulting in high gas-oil ratios and in low oil recoveries, usually in the range of 5 to 25% [3].

The under recovery of this type of reservoirs make them the favorite for secondary recovery applications [4]. The behavior of the saturated gas drive makes the prediction of it recovery a complex one due to continuous changing of the gas and oil viscosities as well as the volume formation factors as a result of the pressure drops. Due to the inherent complexities, a number of simplifying assumptions are advanced to develop simple mathematical models. Several methods including Muskat's method, Schilthius' method, Tracy's method and Tamer's method have appeared in literature for predicting the recovery performance of this type of reservoirs based on rock and fluid properties

The Muskat's method gains a slight advantage over the others as seen in its wide application due to its simplicity. Furtherance to this, the analysis of the reservoir deliverability as to estimate the production rate at any given flowing bottom-hole pressure is a key to forecasting

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reservoir performance[5]. [6] has proposed an empirical inflow performance relationship (IPR) that has been used in the industry successfully. The IPR combined with the vertical tubing (outflow) performance serves as approach to well performance analysis. The objective of this research was to investigate into the effects of tubing size on flow capacity, how cumulative production relates to the decline pressure and time and how average reservoir pressure declines with time.

1.1. Saturated-Gas Drive Reservoirs

This driving form may also be referred to as solution gas drive, dissolved gas drive, internal gas drive and depletion drive mechanisms. In this type of reservoir the principal source of energy is a result of gas liberated from the crude oil and subsequent expansion of the solution gas as the reservoir pressure is reduced below the bubble point pressure. As pressure falls below the bubble point pressure, gas bubbles are liberated within the microscopic spaces[2]. The bubbles expand and force crude oil out of the pore space.[3] suggested that the saturated gas drive can be identified by pressure behavior, water production and unique oil recovery. The reservoir pressure declines rapidly and continuously in saturated gas drives. The decline in the pressure is attributed to the fact that no extraneous fluids or gas cap are available to provide a replacement of the gas and oil withdrawals. There is little or no water production with the oil during the entire producing life of the reservoir. The reservoir is also characterized by rapidly increasing gas-oil ratio from a well, regardless of their structural position. After the pressure has reduced below the bubble point pressure, gas evolves from solution throughout the reservoir. Once the gas saturation exceeds the critical gas saturation, free gas begins to flow toward the wellbore and the gas-oil ratio increases. The gas will also begin a vertical movement due to gravitational forces, which may result in the formation of a secondary gas cap. Oil production is the least efficient recovery method in this drive. The performance of this reservoir is largely described by the gas oil ratio (GOR) as shown in (Fig. 1). In that the GOR tends to remain constant at initial gas solubility (R_{si}) until pressure reaches the bubble point. GOR declines below the bubble point as gas begins to evolve from solution and its saturation increases and begins to flow as gas saturation reaches critical value. Beyond this point the GOR increases rapidly and continuously up to the maximum and then declines to mark the end of the field as pressure depletes completely[4].

1.2. Principal Recovery Models in Dissolved-Gas Drive Reservoirs

Literature is replete with several methods of forecasting the performance of the dissolved-gas drive reservoirs where deterioration of pressure is regarded as a function of GOR,

oil recovery, and produced oil. These methods include Muskat's method, Schilthius' method, Tracy's method and Tarnier's Method. Due to the complexity of this type of reservoirs a number of simplified conventions are made to make their solution reasonably simple[3]. Among them includes the fact that the reservoir is uniform at all times regarding porosity, fluid saturations and relative permeabilities. It is also assumed that uniform pressure exit throughout in both gas and oil zones which implies that gas and oil volume factors, gas and oil viscosities as well as solution gas will remain the same throughout the reservoir. It is further assumed that there is equilibrium at all times between gas and oil phases with negligible gravity segregation forces and negligible water encroachment and production.

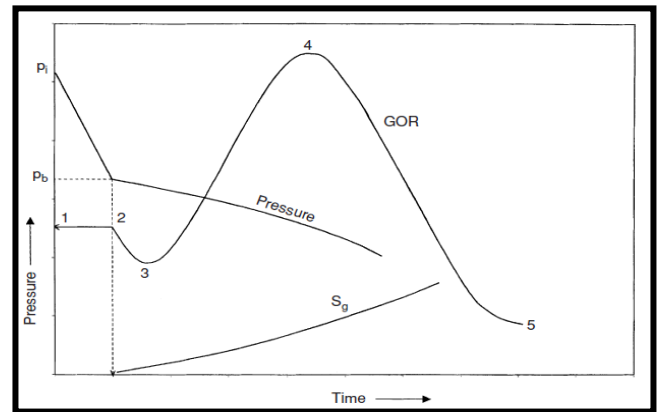


Figure 1. Ideal Production behaviour of a saturated gas-drive reservoir

2. Materials and Methods

Volumetric depletion drive reservoir that exists at its bubble point pressure of 2500 psi with relevant reservoir data provided in Table 1. (Fig. 2) shows the reservoir's total liquid saturation and relative permeability. Also, detailed fluid property data are provided in Appendix 1. Other relevant information includes: Initial Reservoir Pressure ($p_i = p_b$) = 2500 psi, Initial Reservoir Temperature = 180°F, Initial Oil in Place (N) = 56 MMSTB, Initial Water Saturation (S_{wi}) = 0.2 and Initial Oil Saturation (S_{oi}) = 0.8.

Table 1. Available Oil Well Data

Average reservoir pressure	= 2500 psi
Water cut	= 0%
Initial gas – Liquid ratio (GLR _i)	= 721 scf/stb
Productivity index, J*	= 1.5
Gravity	= 25° API
Specific gravity to gas	= 0.7
Average temperature	= 180°F
Wellhead pressure	= 150 psi
horizontal	= 90°
Reservoir depth	= 7500 ft

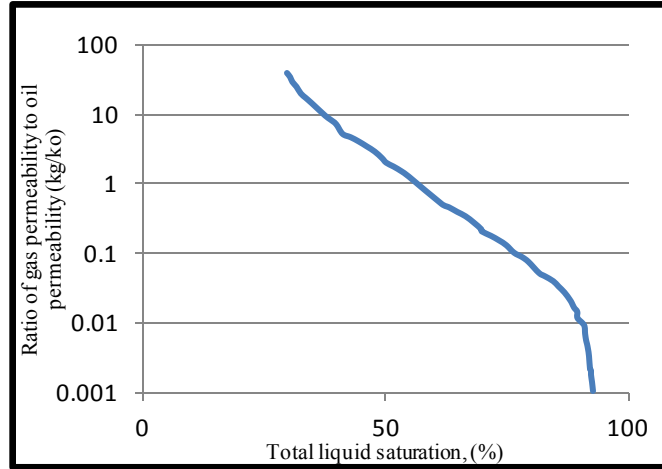


Figure 2. Permeability ratio relationship

2.1. Application of Muskat's Method in Predicting Oil Recovery

Muskat's method was employed in the prediction due to its wide application, simplicity and the size of the available data. In the Muskat's method, the values of the many variables that affect the production of gas and oil and the values of the rate of changes of these variables with pressure are evaluated at any stage of depletion pressure. Assuming these values hold for small drop of pressure, the incremental gas and oil production can be evaluated for these small pressure drops. Muskat expressed the material balance equation for a dissolved drive reservoir in a simplified form as

$$\frac{dS_o}{dp} = \frac{\frac{S_o B_g}{B_o} \frac{dR_{s0}}{dp} + \frac{S_o k_g \mu_o}{B_o k_o \mu_g} \frac{dB_o}{dp} - \frac{(1-S_o-S_w)dB_g}{B_g \frac{dp}{dp}}}{1 + \frac{k_g \mu_o}{k_o \mu_g}} \quad (1)$$

The above equation is simplified further on the account of the pressure functions; as $X(p)$, $Y(p)$ and $Z(p)$.

$$X(p) = \frac{B_g}{B_o} \frac{dR_{s0}}{dp}; Y(p) = \frac{1}{B_o} \frac{\mu_o}{\mu_g} \frac{dB_o}{dp}; Z(p) = \frac{1}{B_g} \frac{dB_o}{dp} \quad (2)$$

Equation 1 takes the form

$$\Delta S_o = \Delta p \left[\frac{S_o X(p) + S_o \frac{k_g \mu_o}{k_o \mu_g} Y(p) - (1-S_o-S_w) Z(p)}{1 + \frac{k_g \mu_o}{k_o \mu_g}} \right] \quad (3)$$

Equation 3 accounts for a change in oil saturation with respect to an incremental drop in pressure. The pressure functions are derived from the reservoir fluid properties. The values of $\frac{dR_{s0}}{dp}$, $\frac{dB_o}{dp}$, and $\frac{dB_g}{dp}$ are derived graphically. Better results are obtained, if values at the middle of the pressure drop interval are used. This is done by simply finding the product of $\frac{\Delta S_o}{\Delta p}$ and the pressure drop Δp , then subtracting the value of ΔS_o from the oil saturation that corresponds to

$$S_{oj} = S_{o(j-1)} - \Delta p \left(\frac{\Delta S_o}{\Delta p} \right) \quad (4)$$

2.2. Instantaneous Gas-Oil Ratio (GOR)

The Produced gas-oil ratio (GOR) at any particular time is the ratio of standard cubic feet of total gas being produced at any time to the stock-tank barrels of oil being produced at

that same time. GOR which is given by equation 5 predicts the reservoir performance at any time in the life of the reservoir.

$$GOR = R_{so} + \frac{k_g \mu_o}{k_o \mu_g} \frac{B_o}{B_g} \quad (5)$$

There are three types of gas-oil ratios; instantaneous gas oil ratio (GOR), solution gas oil ratio (R_s), and cumulative gas oil ratio (R_p). The solution gas oil ratio is given by equation 6.

$$R_p = \frac{G_p}{N_p} \quad (6)$$

$$\therefore G_p = \int_0^{N_p} (GOR) dN_p \quad (7)$$

The incremental cumulative gas produced,

$$\Delta G_p = \int_{N_{p1}}^{N_{p2}} (GOR) dN_p \quad (8)$$

$$\Delta G_p = (GOR)_{avg} \Delta N_p \quad (9)$$

Between N_{p1} and N_{p2} , the above equation can be approximated to:

$$\Delta G_p = \frac{GOR_1 + GOR_2}{2} (N_{p1} - N_{p2}), \text{ or}$$

$$\therefore G_p = \sum (GOR)_{avg} \Delta N_p \quad (10)$$

2.3. The Reservoir Fluids Saturation Equations

The solution of reservoir fluids (oil, gas, and water) in the reservoir at any time is defined as the ratio of volume of the fluid to the pore volume of the reservoir.

$$S_{oi} = \frac{N_{\beta oi}}{P.V} \text{ and}$$

$$S_{oi} = 1 - S_{wi}, \text{ then}$$

$$S_o = \frac{(N - N_p) \times \beta_0}{\frac{N_{\beta oi}}{1 - S_{wi}}} \quad (11)$$

$$S_g = 1 - S_o - S_{wi} \quad (12)$$

The reservoir PVT data must be available in order to predict the primary recovery performance of a depletion-drive reservoir in terms of N_p and G_p . These data are initial oil-in-place (N), hydrocarbon PVT, initial fluid saturations, and relative permeability data. All the techniques that are used to predict the future performance of a reservoir are based on combining the appropriate MBE, with the instantaneous GOR using a proper saturation equation. The

procedure is a repetitive one at series of assumed reservoir pressure drops.

2.4. Inflow Performance Relationship (IPR)

The IPR describes the two phase flow in the porous medium by appropriate models such as Vogel, Fetkovich, Standing, and Wiggins's, The IPR is established by plotting the gross flow rate at different values of the bottom hole flowing pressure. All IPR curves are parallel to each other. The well potential decreases with the decrease in the reservoir pressure and as the pressure inside the reservoir goes below the bubble point gas evolve out of the solution reducing the viscosity of oil[2].

This has the effect of making the formation volume factor greater than one. The combined effect of this is the reduction in the productivity of oil due to the energy which is spent much on moving the liquid and gas phase[7]. The constant productivity index (PI) concept is no longer valid as the pressure is below the bubble point. The Fetkovich empirical correlation was used to estimate the IPR of the reservoir. In the saturated region where $p < p_b$, Fetkovich shows that the (PI) changes linearly with pressure as seen in (Fig. 3).

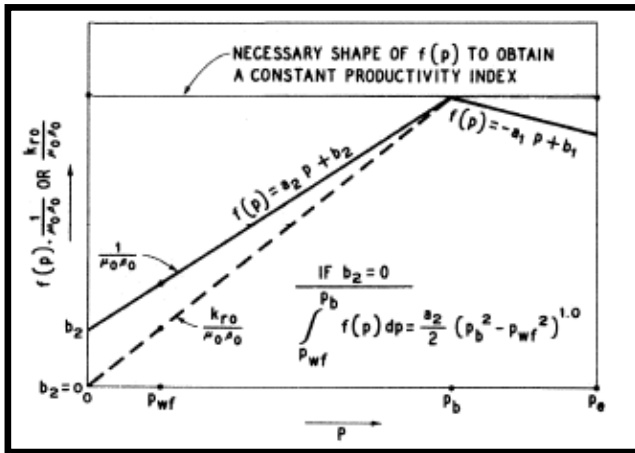


Figure 3. Schematic mobility-pressure behaviors for solution-gas drive reservoirs[Fetkovich, 1973]

2.5. Fetkovich's Correlation

In 1968 Vogel[8] established an empirical relationship for flowrate prediction of solution gas drive reservoirs in terms of the wellbore pressure based on reservoir simulation results. Later[6] proposed a "pressure squared" deliverability relation using pseudo-state theory. When the reservoir pressure p_r and bottom-hole flowing pressure p_{wf} are both below the bubble-point pressure p_b , the pressure function $f(p)$ is represented by the straight-line relationship as expressed by Equation 13.

$$f(p) = \left(\frac{1}{\mu_o \beta_o} \right) \left(\frac{p}{p_b} \right) \quad (13)$$

Equation 13 is expanded to account for the flowrate as pressure declines in field units as shown in equation 14.

$$Q_o = \left[\frac{0.00708 kh}{\ln \left(\frac{r_e}{r_w} \right) - 0.75 + s} \right] \left(\frac{1}{\mu_o \beta_o} \right)_{p_b} \left(\frac{1}{p_b} \right) \int_{p_{wf}}^{p_r} p dp \quad (14)$$

Integrating equation 14 gives

$$Q_o = \left[\frac{0.00708 kh}{\ln \left(\frac{r_e}{r_w} \right) - 0.75 + s} \right] \left(\frac{1}{\mu_o \beta_o} \right)_{p_b} \left(\frac{1}{2 p_b} \right) (p_r^2 - p_{wf}^2) \quad (15)$$

$$Q_{max} = J \left(\frac{1}{2 p_b} \right) (p_r^2 - p_{wf}^2) \quad (16)$$

Where the productivity index $J = \left[\frac{0.00708 kh}{\ln \left(\frac{r_e}{r_w} \right) - 0.75 + s} \right] \left(\frac{1}{\mu_o \beta_o} \right)_{p_b}$

Equation 16 gives the maximum flow rate or the absolute open flow (AOF).

Fetkovich's correlation for the reservoir IPR is much simpler yet theoretically consistent alternative to Vogel IPR formulation. For detail formulations of Vogel see[8]. Fetkovich correlation was considered as it gives better practical applications[9]. Fetkovich deliverability relation is given by equation 17.

$$\frac{Q_o}{Q_{max}} = \left[1 - \left[\frac{p_{wf}}{p_r} \right]^2 \right]^n \quad (17)$$

Where n represent the type of flow; 0.5 for turbulent flow and 1 for laminar flow.

2.6. Tubing Performance Relation (TPR)

The tubing performance or outflow performance represents the vertical flow along the tubing and shows the performance of the well in producing from bottom-hole to the surface. It shows the relationship between the flow rate in tubing and the flowing bottom-hole pressure, and is affected by pressure losses experienced due to restrictions in tubing from chokes, valves and connections. Several methods have been proposed to calculate the bottom-hole pressure of a flowing gas well as it is usually not practical to obtain this pressure directly using a pressure gauge at the bottom of the well.

The least accurate method is the Average Temperature and Deviation Factor method. Poettmann's method also uses a constant temperature but uses a compressibility factor value that varies with pressure making it more accurate and realistic than the Average Temperature and Deviation Method. The Cullender and Smith method uses the least number of assumptions and is widely considered as the most accurate.[10] explained that the Cullender and Smith method is more rigorous than the other methods and "is applicable over a much wider range of gas-well pressures and temperature" since it "makes no simplifying assumptions for the variation of either temperature or Z-factor". The Cullender and Smith method provides a functional relationship between the well flowing bottom-hole pressure (P_{wf}) and the wellhead pressure (P_{wh}) as shown in equation 18.

$$P_{wf} = f(P_{wh}, Q_{well}, T_{wf}, T_{wh}, \text{depth}, ID, \gamma_g, P_{pc}, T_{pc}) \quad (18)$$

where 'Qwell' is the well flow rate, 'Twf' the well bottom-hole temperature, 'Twh' the wellhead temperature, 'depth' the depth of the producing formation from surface, 'ID' the inner diameter of the tubing, 'γg' the specific gravity of the gas, 'Ppc' the critical pressure of the gas, and 'Tpc' the critical temperature of the gas.

Similarly, pressure gradient charts are available in literature and the pressure gradient is related to outflow for outflow performance analysis. A combination of an inflow

performance curve (IPR) and a tubing performance curve (TPR), generally identifies the flow rate and corresponding flowing bottom-hole pressure at a particular reservoir pressure and tubing parameters such as tubing size and wellhead pressure. The deliverability or instantaneous flow rate can then be said to be this combination of the reservoir performance (inflow) and the tubing performance (outflow).

2.7. Prediction of Production and Recovery as a Function of Reservoir Time

Successful evaluation of the exact value of average reservoir pressure per the producing capacity or deliverability is essential for effective resource management. The period to put the well on artificial lift (gas lift) as a function of decline in production capacity relative to the reservoir time is crucial for effective economic analysis of the field. The incremental time required to support incremental cumulative production is given by equation 19.

$$\Delta t = \frac{\Delta N_p}{Q_{o(avg)}} \quad (19)$$

$$t = \sum \Delta t \quad (20)$$

Hence the cumulative production is given by

$$N_p = \sum \Delta N_p \quad (21)$$

2.8. Production Optimization by Artificial Lift

During the life of a producing field, static reservoir pressure may not be in adequate amount to lift economic flow-rates through the wellbore and overcome surface pressure restrictions. Artificial lift systems objective is to reduce bottom hole flowing pressure, net hydrostatic gradient and increase flow rate by injecting gas lift to the down hole produced fluids. Numerous articles related to flow and artificial lift can be found in literature.

A few of these examples are cited in the references[11, 12, 13, 14]. As reservoir conditions change with time, artificial lift quantities (gas lift flow, compressor power, pump head, or pump strokes) have to adjust in order to maintain proper fluid production. A continuous depletion of reservoir pressure will cause the bottom hole flowing pressure level sufficiently low as to make the conventional lifting (spontaneous production) inefficient and uneconomic.

3. Results and Discussions

3.1. Hydrocarbon Recovery and Optimization by Artificial Lift

During the life of a producing field, static reservoir pressure may be inadequate amount to lift economic flow-rates through the wellbore and overcome surface pressure restrictions. A continuous depletion of reservoir pressure will cause the bottom hole flowing pressure level sufficiently low as to make the conventional lifting (spontaneous production) inefficient and uneconomic.

As pressure continues to decline below the bubble point pressure there is a corresponding evolving and production of

gas precipitating the reservoir into depletion as shown in (Fig. 4). The amount of hydrocarbon that can be recovered at any forecasting pressure (N_p and G_p) can be easily determined. At abandonment pressure of 100psia, there is only about 18.7% of the stock tank oil initially in place which can be recovered through conventional lifting (Fig. 5). This information is particularly important for the quick response of surface facilities by artificial lift to handle production in a more suitable and economical advantage. Through the artificial lift, the reservoir pressure is kept constant, or there is some compensation in the pressure drop due to production.

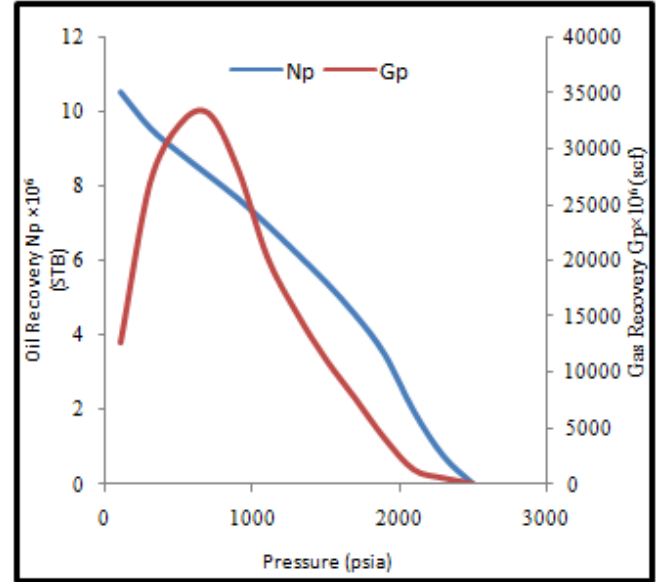


Figure 4. Production performance as a function of decline pressure

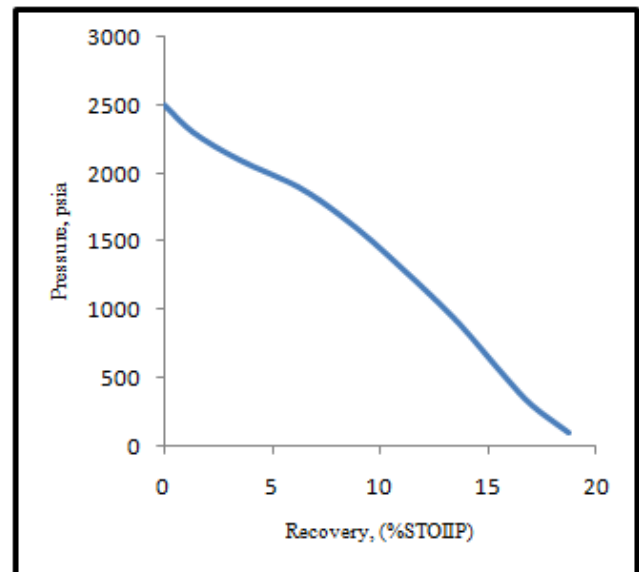


Figure 5. Average reservoir pressure as a function of cumulative oil production

3.2. The Solution Gas Oil Ratio and Average Gas Oil Ratio

Fig. 6 shows the relation between solution gas oil ratio (R_s) and the average gas oil ratio R_{av} calculated against reservoir

pressure. The R_{av} is increasing to a maximum value of about 4003 scf/STB at reservoir pressure 700psia. The increasing gas oil ratio is fairly responsible for the low recovery as in the case studied since there is a corresponding increase in gas mobility reducing oil mobility. This is attributed to larger number of gas bubbles as also indicated by[15].

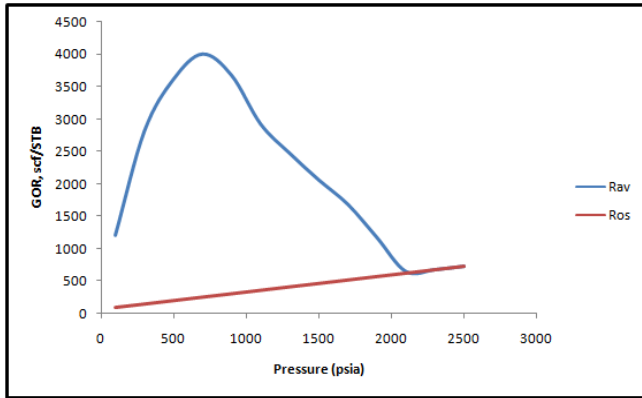


Figure 6. Produced and solution gas oil ratios as a function of decline pressure

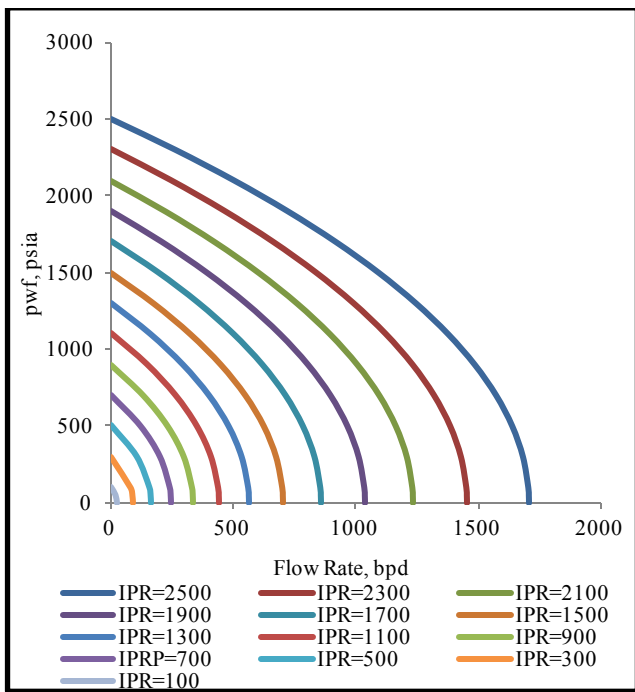


Figure 7. Fetkovich saturated future IPRs

3.3. Performance of the Reservoir (IPR)

The performance of the reservoir at any time in the future is crucial in the resource management. The IPR describes the two phase flow in porous medium by Fetkovich model at any average reservoir pressure (Fig. 7). The IPR is established by plotting the gross flow rate at different values of bottom hole flowing pressure. The maximum flow rate obtainable from the analysis is about 1710 bpd. All IPR curves are parallel to each other. The well potential decreases with the decrease in reservoir pressure. The intercept IPR curves with y-axis gives the average reservoir pressure. For the case considered

the inflow mobility (λ) of the reservoir as a function of formation pressure (p_{wf}) is given as $\lambda(p_{wf}) = 7E-08p_{wf}^2 + 0.0002p_{wf} + 0.6$. This confirms the validity of solution gas reservoirs that below the bubble point that their productivity is not constant as supported by[16]. The function makes determination of any future inflow mobility feasible.

3.4. Effect of Tubing String on Flow Capacity

The size of the production tubing can play an important role in the effectiveness with which the well can produce liquid[17]. There is an optimum tubing size for any well system[18]. Smaller tubing sizes have higher frictional losses and higher gas velocities which provide better transport for the produced liquids. Larger tubing sizes, on the other hand, tend to have lower frictional losses, pressure drops due to lower gas velocities and in turn lower the liquid carrying capacity[17].

Too large tubings will cause a well to load up with liquids and die[18]. (Fig. 8) is plot of the outflow performance relationship (OPR) of the various tubing sizes superimposed on the IPR curves. It is observed that the smaller size tubings have excessive frictional losses with low production rates thereby restricting production. Four larger size tubings (2", 2½", 3" and 4") are considered to be the better candidates to start producing the well. However, the 4" tubing exhibits the lowest frictional loss which might cause the well to load up with liquids and die too early. The 2½" tubing gives a much more reasonable frictional loss as compared to that of 4" and 2" tubings with an equilibrium production rate of about 1200 bpd and an equivalent bottom-hole flowing pressure of about 1350 psi see (Fig. 8).

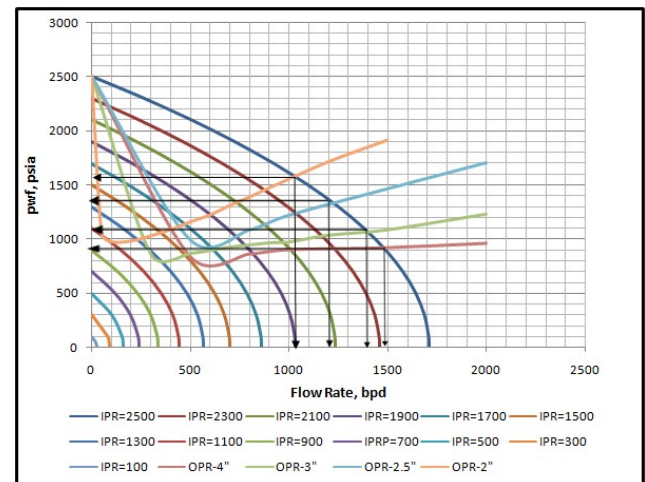


Figure 8. Plot of IPRs and OPRs for the various tubing sizes

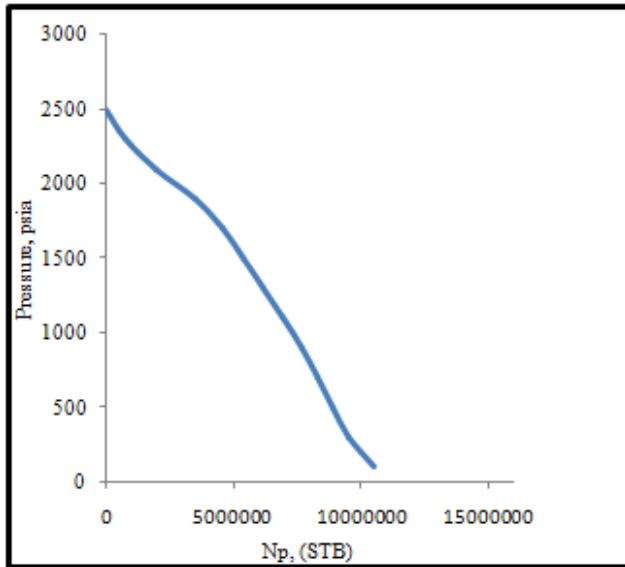
The point of intersection of the well flow rate and the flowing bottom hole pressure and the well tubing performance gives operating points of the various tubing sizes are shown in Table 2. 2½" tubing was chosen to produce the reservoir from the initial average reservoir pressure of 2500 psia at a GOR of 721 scf/STB up to about 1700 psia with production capacity of 1200bpd. Beyond this point appropriate velocity string would be needed.

Table 2. Equivalent flow capacities of larger tubing sizes

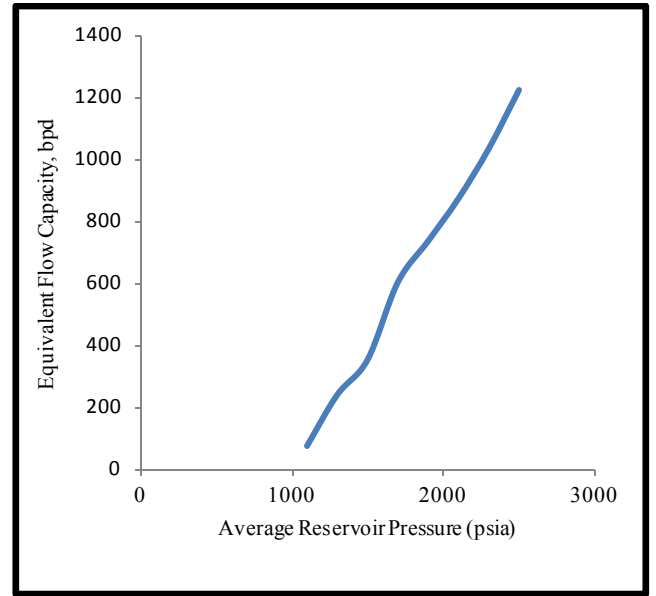
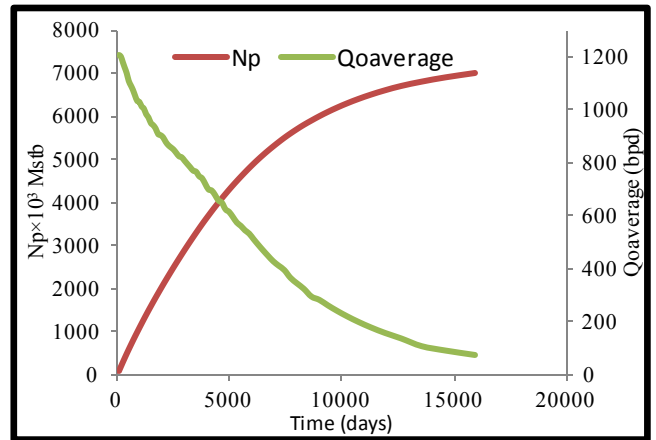
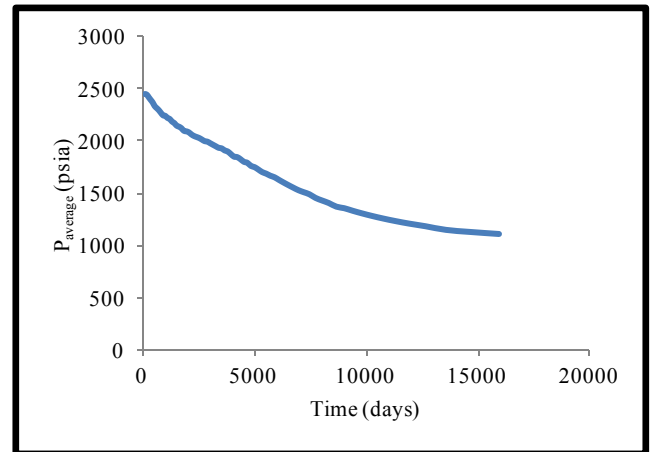
Tubing size (inches)	Bottom-hole pressure (psia)	Producing capacity, (bpd)
2"	1550	1040
2.5"	1350	1200
3"	1050	1300
4"	900	1485

3.5. Forecasting Production and Recovery at Any Future Reservoir Time

Predicting the average reservoir pressure at which the producing capacity will decline to leading to abandonment is very crucial. The reservoir development, planning and successful economic evaluations depends on this data and its availability as a function of time is equally important. The time to place the well on artificial lift and time to install pump or compressors when certain producing capacities can no longer be met is very necessary[16]. To do this the incremental oil recovery ΔN_p and the corresponding average pressure P_{avg} are determined from (Fig. 9). The average pressure is then applied on the (Fig. 10) to determine the corresponding average equivalent production capacity Q_{oavg} . The incremental time Δt , the total time t and the cumulative production N_p are determined using equation 19, 20 and 21 respectively.

**Figure 9.** Average reservoir pressure as a function of cumulative oil production

The result of the performance of the field is shown in (Fig. 11). The flow capacity of the field reaches 77 bpd at about 15925 days. Beyond this point pumping will start to optimize the production levels. For detail of the performance analysis see appendix 3. The distribution of the average reservoir pressure over time is shown in (Fig. 12). The reservoir pressure depletion continues up to a region of about 1100 psia. The cumulative oil produced at the abandonment is approximately 7000000Mstb.

**Figure 10.** Equivalent flow capacity as a function of decline pressure**Figure 11.** Production performance as a function of time**Figure 12.** Average reservoir pressure as a function of time

4. Conclusions

From the analysis in this paper it can be concluded that saturated-gas drive reservoirs are best candidates for

secondary recovery applications due to their low ultimate recovery, about 18% of STOIIP for the case considered. This is explained in the fact that as pressure declined rapidly gas mobility becomes larger with reducing oil mobility due to increasing oil viscosity and hence decreasing oil permeability leading to high gas-oil ratio. Again it has been confirmed that the productivity index also known as mobility index below the bubble point ceases to be constant. It is observed that the outflow performance of a well is largely proportional to the tubing size. The smaller size tubings have excessive frictional losses with low production rates thereby restricting production. Large size tubing exhibits the lowest frictional loss yet their use might cause the well to load up with liquids and die too early.

The 2½" tubing gives a much more reasonable frictional

loss as compared to that of 4" and 2" tubings with an equilibrium production rate of about 1200 bpd and an equivalent bottom-hole flowing pressure of about 1350. From the IPR analysis the maximum inflow rate obtainable is 1710bpd with an outflow rate of 1200bpd. The flow capacity near abandonment reaches 77bpd at about 15925days with cumulative oil produced estimated at 7MMstb. Combination between material balance equation (Muskat model), the Fetkovich inflow performance relationship model of flow through porous medium and the tubing outflow performance relationship makes an easily forecasting oil production rate. The case considered set out the theoretical framework for the evaluation of the performance and future prediction of saturated gas drive reservoirs.

Appendixs

Appendix 1: Fluid Property Data

Pressure (psia)	B _o bbl/STB	R _{so} SCF/STB	B _g bbl/SCF	U _o cp	U _g cp
2500	1.498	721	0.00105	0.488	0.017
2300	1.463	669	0.00116	0.539	0.0166
2100	1.429	617	0.00128	0.595	0.0162
1900	1.395	565	0.00144	0.658	0.0158
1700	1.361	513	0.00163	0.726	0.0154
1500	1.327	461	0.00188	0.802	0.015
1300	1.292	409	0.00221	0.887	0.0146
1100	1.258	357	0.00265	0.982	0.0142
900	1.224	305	0.0033	1.085	0.0138
700	1.19	253	0.00432	1.199	0.0134
500	1.156	201	0.00616	1.324	0.013
300	1.121	149	0.01047	1.464	0.0126
100	1.087	97	0.03203	1.617	0.0122

Appendix 2: Results of the Muskat Primary Prediction Method for the Reservoir

Pressure (psia)	N _p (STB)	GOR (scf/STB)	G _p (scf)	N _p /N	Recovery (%STOIIP)
2500	0	721		0	0
2300	7.46E+05	669.4113	4.99E+08	0.013326	1.332604
2100	1.94E+06	662.5962	1.24E+09	0.034704	3.470426
1900	3.48E+06	1769.111	4.06E+09	0.062155	6.215458
1700	4.54E+06	2846.411	7.62E+09	0.081058	8.105808
1500	5.41E+06	3652.632	1.11E+10	0.096693	9.669333
1300	6.19E+06	4528.873	1.53E+10	0.110601	11.06014
1100	6.96E+06	5484.704	2.03E+10	0.124207	12.42068
900	7.67E+06	7044.934	2.82E+10	0.136886	13.6886
700	8.28E+06	7754.631	3.32E+10	0.147929	14.79292
500	8.89E+06	7022.99	3.21E+10	0.158812	15.88119
300	9.56E+06	5470.842	2.69E+10	0.170785	17.07854
100	1.05E+07	2302.474	1.26E+10	0.187859	18.7859

Appendix 3: Result of Performance as a Function of Time

$\Delta N_p \times 10^3$ (STB)	$N_p \times 10^3$ (STB)	$P_{average}$ (psia)	$Q_{o, average}$ (bpd)	Δt (days)	t (days)	Tubing String
100	100	2457	1203	83.11	83.11	2.5"
100	200	2450	1197	83.51	166.62	2.5"
100	300	2425	1177	84.99	251.60	2.5"
100	400	2400	1156	86.52	338.12	2.5"
100	500	2375	1135	88.11	426.23	2.5"
100	600	2340	1106	90.43	516.65	2.5"
100	700	2320	1089	91.81	608.46	2.5"
100	800	2300	1073	93.23	701.70	2.5"
100	900	2274	1051	95.15	796.85	2.5"
100	1000	2250	1031	97.00	893.84	2.5"
100	1100	2245	1027	97.39	991.23	2.5"
100	1200	2225	1010	98.99	1090.23	2.5"
100	1300	2215	1002	99.81	1190.04	2.5"
100	1400	2190	981	101.93	1291.97	2.5"
100	1500	2175	969	103.24	1395.21	2.5"
100	1600	2150	948	105.51	1500.72	2.5"
100	1700	2140	939	106.44	1607.16	2.5"
100	1800	2125	927	107.87	1715.04	2.5"
100	1900	2100	906	110.35	1825.39	2.5"
100	2000	2095	902	110.86	1936.24	2.5"
100	2100	2085	894	111.89	2048.13	2.5"
100	2200	2065	877	114.01	2162.14	2.5"
100	2300	2050	865	115.65	2277.79	2.5"
100	2400	2040	856	116.78	2394.57	2.5"
100	2500	2030	848	117.92	2512.49	2.5"
100	2600	2015	836	119.68	2632.17	2.5"
100	2700	2000	823	121.49	2753.66	2.5"
100	2800	1995	819	122.11	2875.77	2.5"
100	2900	1980	806	124.00	2999.76	2.5"
100	3000	1965	794	125.94	3125.71	2.5"
100	3100	1950	782	127.95	3253.66	2.5"
100	3200	1935	769	130.02	3383.68	2.5"

Appendix 3 Result of Performance as a Function of Time continued

$\Delta N_p \times 10^3$ (STB)	$N_p \times 10^3$ (STB)	$P_{average}$ (psia)	$Q_{o, average}$ (bpd)	Δt (days)	t (days)	Tubing String
100	3300	1930	765	130.73	3514.41	2.5"
100	3400	1910	748	133.63	3648.04	2.5"
100	3700	1850	698	143.16	4065.37	2.5"
100	4100	1790	649	154.16	4663.31	2.5"
100	4200	1760	624	160.31	4823.63	2.5"
100	4300	1748	614	162.92	4986.54	2.5"
100	4400	1725	595	168.14	5154.69	2.5"
100	4500	1700	574	174.22	5328.91	2.5"
100	4600	1685	562	178.08	5506.99	2.5"
100	4700	1665	545	183.51	5690.50	2.5"
100	4800	1650	532	187.80	5878.29	2.5"
100	4900	1625	512	195.41	6073.70	2.5"
100	5000	1600	491	203.66	6277.36	2.5"
100	5100	1575	470	212.64	6489.99	2.5"
100	5200	1550	450	222.44	6712.44	2.5"
100	5300	1525	429	233.19	6945.63	2.5"
100	5400	1505	412	242.57	7188.20	2.5"
100	5500	1485	396	252.74	7440.94	2.5"
100	5600	1450	367	272.74	7713.68	2.5"
100	5700	1425	346	289.07	8002.75	2.5"
100	5800	1400	325	307.48	8310.23	2.5"
100	5900	1365	296	337.59	8647.82	2.5"
100	6000	1350	284	352.37	9000.19	2.5"
100	6100	1325	263	380.10	9380.29	2.5"
100	6200	1300	242	412.58	9792.86	2.5"
100	6300	1275	222	451.11	10243.97	2.5"
100	6400	1250	201	497.57	10741.55	2.5"
100	6500	1225	180	554.70	11296.25	2.5"

100	6600	1200	160	626.64	11922.90	2.5"
100	6700	1175	139	720.01	12642.91	2.5"
100	6800	1140	110	909.76	13552.67	2.5"
100	6900	1120	93	1071.02	14623.69	2.5"
100	7000	1100	77	1301.74	15925.44	2.5"

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