

Dynamic Effect of the Intermediate Block in a Hydraulic Control System

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Abstract The intermediate block is a basic element in an hydraulic control system, and is usually used to install all hydraulic components and guides the fluid flows. However, the effect of this block is usually neglected, but it has to be taken into consideration when high performance applications, especially at high frequencies, have to be achieved. This paper focuses on this component and shows how it can influence the hydraulic system dynamics. The main contributions of this work are the implementation of a Bond Graph model of this component, which can easily be integrated in the whole system model, and a complete analysis of the effects (pressure drop, compressibility, inertia) induced by the intermediate block on the whole system performances. The relationship between flow rates and pressure drops along with the energy losses in the block are obtained according to a method based on the decomposition of the circuit in parts for which the local losses can be obtained from abacuses. The Computational Fluid Dynamics (CFD) is used for the validation of the results. Besides, the compressibility and inertial effects are carefully studied since they have a great influence on the hydraulic frequency. Finally, simulations and experiments are implemented for demonstrating the importance of the effect of the intermediate block in the hydraulic system modeling. By introducing compressibility and inertial effects of the intermediate block, the simulation result shows better agreement with experimental results at high frequencies. This comparison demonstrates that the control design can reach better performance when considering the dynamic model of the intermediate block.

Keywords Intermediate Hydraulic Block, CFD, Bond Graph, Energy Dissipation, Compressibility Effect, Inertia Effect

1. Introduction

In a typical hydraulic control system, the displacement of the actuator is piloted via a control element, such as a servovalve, which is connected to the actuator by an intermediate block. Moreover, most of the other hydraulic components required by the application are also installed on this block, for example accumulators, pressure sensors, electrovalves, flow reducers, etc.. This can lead to complex intermediate blocks, which may influence the whole system dynamics. Figure 1 shows the configuration of the inner circuit of the intermediate block in our test rig. The oil from the hydraulic pump is guided into the block after a filter, and then redirected towards the servovalve. Controlled by the servovalve, the flow is supplied to the actuator through the block. Besides, the block enables the system to alternate between three different working modes via the commutation of two electrovalves (V20 and V21):

- Mode 1: a single 4-way servovalve to control the actuator;

- Mode 2: two 4-way servovalves in parallel to control the actuator;

- Mode 3: two 4-way servovalves with each servovalve used as a 3-way component to control the flow in one actuator chamber each.

According to the working mode, the oil flows in different passages and crosses several inner tubes.

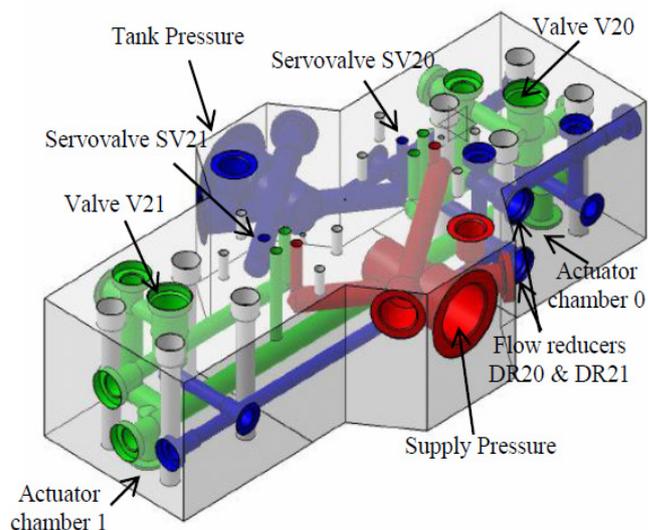


Figure 1. Configuration of the inner tubes

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Published online at <http://journal.sapub.org/jmea>

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Most of previous studies dealing with the dynamics analysis of hydraulic servovalves and actuators[1-5] make the assumption that the effect of the intermediate block could be neglected. This assumption is reasonable for most of the conventional applications at low frequency. But for high frequency systems, this assumption becomes invalid and leads to inaccurate results. As indicated in the supplier's literature, the MOOG D765 servovalves used in the system under study have a bandwidth which can reach 500 Hz for 5% of the spool displacement with a rated flow up to 19 l/min at 70 bar pressure drop and full opening. The total inner volume of the block under consideration reaches 0.2 liter. Compared to the total actuator volume of 0.3 liter, it would influence the dynamics behavior of the hydraulic control system at high frequencies. Therefore, it makes sense to establish a dynamic model of the intermediate block in the aim to integrate it into the whole system model. This would be helpful to study the performances of the hydraulic control system at high frequencies. The main contribution of this paper is to focus on the modeling of intermediate block and to show how it may influence the hydraulic performances due to induced losses, compressibility and inertial effects. According to this study, the control performance will be finally improved, especially at high frequencies where the effect of the intermediate block volume and that of the fluid inertia in the block are involved and have a significant effect.

The modeling tool applied here to develop a dynamic model for the intermediate block is the Bond Graph modeling language[6]. This is a powerful methodology for handling complex and multidisciplinary systems with a unified graphical and mathematical form. Because of its clear architecture and flexibility to diverse problems, this method is widely adopted in various domains, i.e. mechanics[7, 8], hydraulics[9-11], thermodynamics[12, 13], robotics[14-16], etc.. With Bond Graph, the model of the intermediate block can finally be integrated into the Bond Graph model of the whole system already including a detailed model of the servovalve[17] in the range of 0 to 200 Hz working frequencies.

The model of the intermediate block should deal with the flow energy losses which are very complex. In the field of the fluid dynamics, most problems yield to nonlinear and differential representations to get an accurate result. A first way to calculate these losses is to use the Computational Fluid Dynamics (CFD) analysis. This numerical approach is based on the discretization of space and time, the continuous variables being turned to a finite set of nodal values and interpolating functions. Then, the original problem becomes an algebraic one that can be solved by computer. This method has been applied here for calculating the pressure drop in the different passages of flow in the intermediate block. However, the CFD simulation is still not usable for the simulation of the dynamics of such a system[18, 19].

This paper proposes then a method to obtain the losses parameters of the lumped-parameter model of the block based on the Bond Graph representation. It consists in

considering that the inner circuits of the block are made up of associations of basic hydraulic resistance elements such as tubes, bends and bifurcations. The energy losses are then calculated using formulae and abacuses from literature for determining the pressure loss coefficients for each basic element[20, 21]. In the following, this method is called "abacus-based method" (ABM). The CFD method is then used to bring a comparison and validate the results of the proposed method.

In order to take the dynamic effect of the intermediate block into consideration, Section 2 of this paper will describe the modeling approach applied to represent accurately the intermediate block. Section 3 will introduce CFD and abacus-based methods to find the function of the energy dissipation due to the fluid flow in the block, and their results will be compared. Section 4 and 5 will study respectively the compressibility and inertial effects of the intermediate block. Some frequency response results of the simulation and experiment will be addressed in section 6 so as to demonstrate the importance of the dynamic effect of the intermediate block. Finally, section 7 will give some conclusions.

2. Modeling of the Intermediate Block

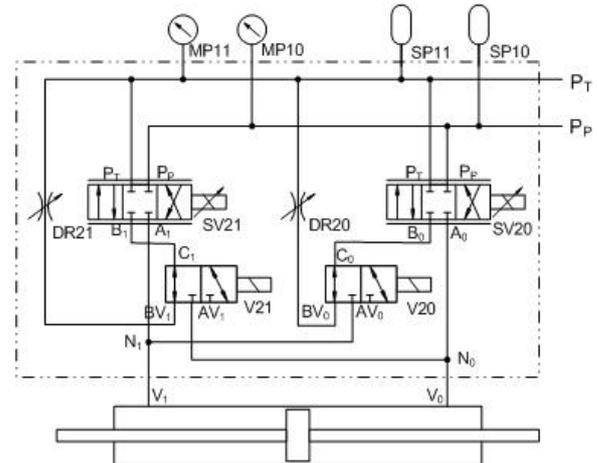


Figure 2. Scheme of the hydraulic control system setup

A scheme of the electro-hydraulic control system setup is shown in Figure 2. All components are connected on the intermediate block which guides the fluid flow according to the selected mode. The control of the electrovalves V20 and V21 allows the system to switch between the three working modes as described in the introduction.

When both electrovalves are in ON-position and the control input of one servovalve is set to 0, the control of the actuator corresponds to conventional hydraulic applications. However, in this configuration, both servovalves can be simultaneously controlled, this lead to a parallel 4-way mode which can provide a greater flow rate to the actuator. Finally, when both electrovalves are in OFF-position, the servovalves are used in 3-way mode, i.e., only one outlet port of each servovalve is connected to a chamber of the actuator.

These two last modes enable the use of multivariable control strategy.

The analysis done in this paper focuses on the study of this block circuit connecting the outlet ports A and B of the servovalves and the ports V_0 and V_1 of the actuator. Five passages are then taken into consideration:

- 1) Passage A_i-N_i : from the port A_i of servovalve SV2i to the bifurcation N_i ;
- 2) Passage N_i-V_i : from the bifurcation N_i to the port V_i of the chamber of the actuator;
- 3) Passage B_i-C_i : from the port B_i of the servovalve SV2i to port C_i of the electrovalve V2i;
- 4) Passage C_i-N_i : from the port C_i of the electrovalve V2i (when the valve is ON) to the bifurcation N_i ;
- 5) Passage C_i-P_T : from the port C_i of the electrovalve V2i (when the valve is OFF) to the tank (passing through the flow reducer).

The diagram of the distribution of passages is presented in Figure 3.

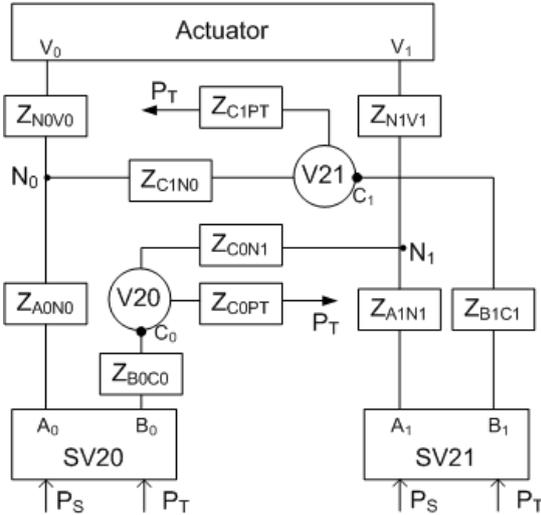


Figure 3. Diagram of the different passages of the intermediate block

While considering only the effect of the intermediate block, the influence of the losses in electrovalves and flow reducers are neglected as the flow passes through these components without bend or section change.

Each passage (noted Z in Figure 3) is modeled considering three effects: the energy dissipation (pressure drop), the compressibility, and the fluid inertia. These enable the representation of the first frequency mode for each passage.

Figure 4 (a) shows the corresponding Bond Graph representation of a passage. The energy dissipation effect is represented by a resistor (R-element), all energy losses throughout each part of the passage being considered as a single pressure drop. These losses include the singular losses due to the local geometry (change of direction or flow area), and the frictional losses caused by the fluid viscosity. The total energy loss can be expressed as a function of the flow rate (1):

$$\Delta P = f(Q) \quad (1)$$

This relation will be fully developed in the next section by the means of CFD analysis and ABM.

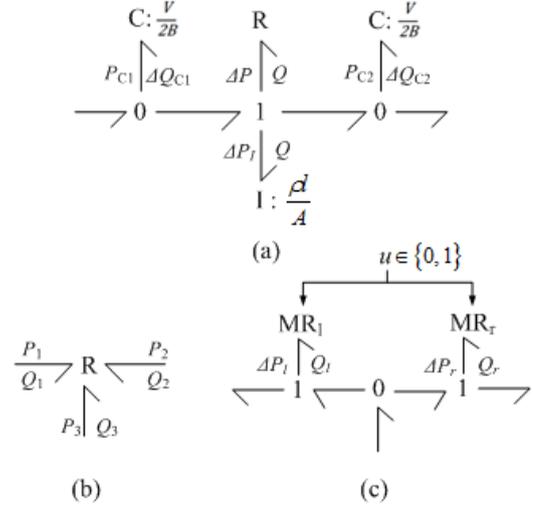


Figure 4. Bond Graph model of (a) a passage, (b) a bifurcation and (c) a valve

The fluid compressibility effect is represented by capacitors (C-elements) placed on both sides of the R-element, splitting the fluid volume of the passage into two identical volumes for model causality reason. The constitutive equation of these C-elements can be written as:

$$\frac{dP_C}{dt} = \frac{2B}{V} \cdot \Delta Q_C \quad (2)$$

where B is the bulk modulus, and V is the whole passage volume.

The fluid inertia effect (I-element) is related to the kinetic energy of the fluid in the passage under consideration. The corresponding constitutive relationship is given by:

$$\frac{dQ}{dt} = \frac{A}{\rho l} \cdot \Delta P_l \quad (3)$$

where l is the passage length; ρ is the fluid density; A is the equivalent section area derived from the ratio of the passage total volume and length.

A bifurcation N combines two passages together. This component can be represented by a 3-port R-element as shown in Figure 4 (b). No matter which two flow rates among the three are given, the pressure drop can be calculated according to abacus-based method according to the geometric dimensions of the bifurcation. Details will be given in the next section.

Due to the choice made for the electrovalves, the pressure losses in these components can be neglected, and they are considered to have ideal properties. As shown in Figure 4 (c), each valve is modeled by a modulated resistor (MR-element) which is controlled by a two-state command ($u \in \{0, 1\}$). The constitutive equation of the MR-element on the left side (Figure 4 (c)) is as follows:

$$\begin{cases} Q_l = 0, & u = 0 \\ \Delta P_l = 0, & u = 1 \end{cases} \quad (4)$$

The equation of MR-element on the right side takes the same values but for the opposite command values in (4).

Finally, the Bond Graph model of the intermediate block is established by integrating all passages and bifurcations models. The final model is shown in Figure 5. In this model, the compressibility and inertia effects of the passage Z_{A0N0} are neglected due to its small volume (nearly $2 \cdot 10^{-6} \text{ m}^3$).

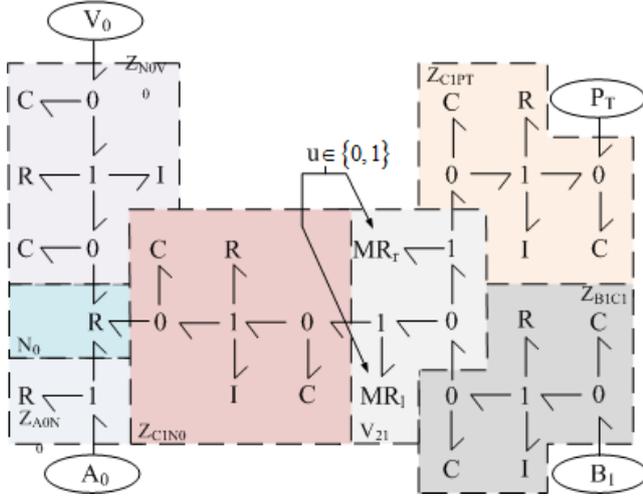


Figure 5. Bond Graph model of the intermediate block for controlling a side of the actuator volume

3. Energy Dissipation Calculation by Abacus-Based and CFD Methods

The relationship between the flow rate and the pressure drop is complex in hydraulic systems. The energy dissipation depends not only on the local geometry and the fluid properties, but also on the Reynolds number which is a

function of the flow velocity. It does not exist a unified formula valid for all cases. The CFD analysis enables to obtain the energy dissipation in the intermediate block but this method is difficult to apply for a lumped parameter approach. Indeed, boundary conditions to be set in the numerical model are not straightforward for the inner passages as these conditions change according to what happens in all the other passages. CFD is used here only to validate the results of the abacus-based method. This is done by comparing flow rates and pressure drops characteristics for each passage and their combinations.

The CFD approach is used to determine the relationship of the flow rates and pressure drops with 3D geometric models. All passages mentioned in the previous section are exactly modeled and meshed. The boundary conditions are inlet and outlet pressure type for the single-input and single-output passages. Inlet velocity and outlet pressure boundary conditions are imposed to the bifurcations or to the passages containing a bifurcation so that the flow rate is determined at each port. Since the Reynolds number in the block is lower than 5000, laminar conditions are considered for the calculation.

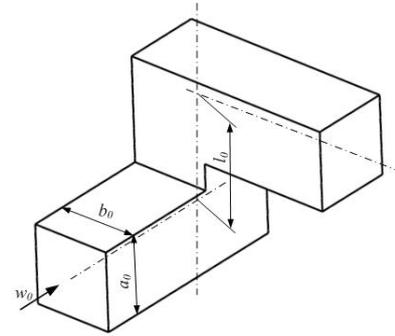


Figure 6. Element formed by two bends assembled at an angle of 90°

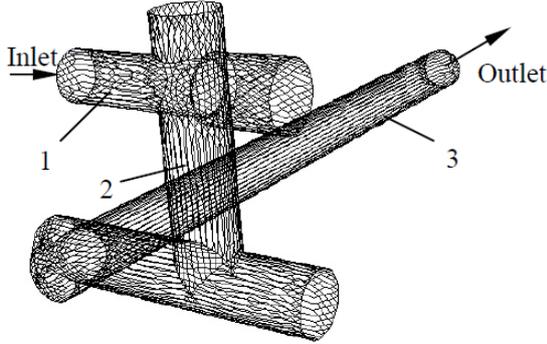
Table 1. Calculation of the Pressure Loss Coefficient According to ABM

No.	Resistance composition	Type of resistance	Principal dimension	Characteristic parameter	ζ_{total}
1	Tube 1	Straight tube	Length: $l_1 = 28 \text{ mm}$ Diameter: $D_1 = 12 \text{ mm}$	$\frac{l_1}{D_1} = \frac{28}{12} = 2.33$	$\frac{64}{Re} \cdot \frac{l_1}{D_1} = \frac{149.12}{Re}$
2	Tube 2	Straight tube	Length: $l_2 = 46 \text{ mm}$ Diameter: $D_2 = 15.2 \text{ mm}$	$\frac{l_2}{D_2} = \frac{46}{15.2} = 3.03$	$\frac{64}{Re} \cdot \frac{l_2}{D_2} = \frac{193.92}{Re}$
3	Tube 3	Straight tube	Length: $l_3 = 212 \text{ mm}$ Diameter: $D_3 = 15 \text{ mm}$	$\frac{l_3}{D_3} = \frac{212}{15} = 14.13$	$\frac{64}{Re} \cdot \frac{l_3}{D_3} = \frac{904.32}{Re}$
4	Junction of tube 1 and 2	Resistance with two bends at 90°	Tube 1 diameter: $D_1 = 12 \text{ mm}$ Tube 2 diameter: $D_2 = 15.2 \text{ mm}$ Axis distance: $l_4 = 5 \text{ mm}$	$\frac{l_4}{D_1} = \frac{5}{12} = 0.42^b$	$2.44 \times 1.2 + \frac{64}{Re} \cdot \frac{l_4}{D_1} = 2.93 + \frac{26.88^c}{Re}$
5	Junction of tube 2 and 3 ^a	Resistance with two bends at 90°	Tube 2 diameter: $D_2 = 15.2 \text{ mm}$ Tube 3 diameter: $D_3 = 15 \text{ mm}$ Axe distance: $l_5 = 45 \text{ mm}$	$\frac{l_5}{D_3} = \frac{45}{15} = 3^b$	Q from 2 to 3: $3.17 + \frac{64}{Re} \cdot \frac{l_5}{D_3} = 3.17 + \frac{192}{Re}$ Q from 3 to 2: $3.17 \times 1.2 + \frac{64}{Re} \cdot \frac{l_5}{D_3} = 3.80 + \frac{192^c}{Re}$

a. The losses of the tube between 2 and 3 are considered in those of the junction.
 b. As an approximation, the smallest value of both diameters is taken for calculation
 c. Bend with recess.

Table 2. Calculation of the Pressure Drop

Flow rate (l/min)	Pressure drop (bar): $\Delta P = \zeta_{total} \cdot \rho/2 \cdot (Q/A_0)^2$					
	Element 1 $A_0 = 113.10 \text{ mm}^2$	Element 2 $A_0 = 181.46 \text{ mm}^2$	Element 3 $A_0 = 176.71 \text{ mm}^2$	Element 4 $A_0 = 113.10 \text{ mm}^2$	Element 5 $A_0 = 176.71 \text{ mm}^2$	Total pressure drop
30	0.00748	0.00478	0.02320	0.24455	0.11236	0.39237
20	0.00499	0.00318	0.01547	0.10899	0.05097	0.18360
10	0.00249	0.00159	0.00774	0.02747	0.01352	0.05281
0	0	0	0	0	0	0
-10	-0.00249	-0.00159	-0.00774	-0.02747	-0.01352	-0.05281
-20	-0.00499	-0.00318	-0.01547	-0.10899	-0.05097	-0.19318
-30	-0.00748	-0.00478	-0.02320	-0.24455	-0.11236	-0.41391

**Figure 7.** Geometric model of the passage Z_{C0N1}

For the abacus-based approach, each passage under study is divided into basic hydraulic resistances, such as tubes, bends and bifurcations. The pressure drop of each basic element is calculated from the following equation[20]:

$$\Delta P_{total} = \zeta_{total} \cdot \frac{\rho w_0^2}{2} = \zeta_{total} \cdot \frac{\rho}{2} \cdot \left(\frac{Q}{A_0} \right)^2 \quad (5)$$

where ζ_{total} is the global pressure loss coefficient of a resistance element; w_0 is the flow velocity in the element; A_0 is the section area of the element.

The global pressure loss coefficient depends on the flow conditions by the Reynolds number, on the shape of the resistance element, and on the geometric dimensions. For the calculation of the pressure drop, it is just necessary to determine the global pressure loss coefficient by applying the empirical formulae or abacuses given in the literature[20, 21].

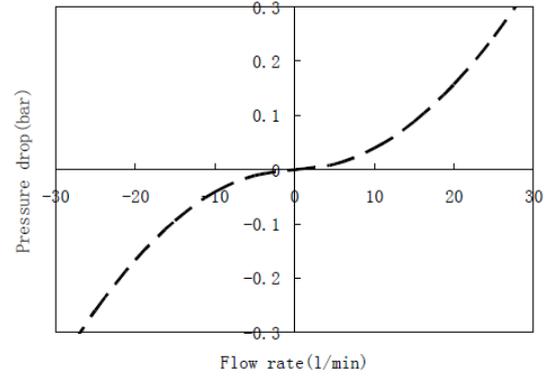
For example,[20] gives the following empirical formula for an element formed by two bends of same section area A_0 assembled at an angle of 90° (see in Figure 6):

$$\zeta_{total} = C_I \zeta_M + \zeta_f \quad (6)$$

where C_I is a constant depending on the form of the tube; ζ_M is the frictional loss coefficient due to the fluid viscosity; ζ_f is the singular loss coefficient in the local resistance place. C_I and ζ_M are obtained according to the abacuses in[20], ζ_f is given by:

$$\zeta_f = \frac{64}{\text{Re}} \cdot \frac{l_0}{D_H} \quad (7)$$

where l_0 is the distance between the axes of two consecutive bends; D_H is the hydraulic diameter of the tube. Finally, the pressure drop for this element can be calculated by (5).

**Figure 8.** ABM results of pressure drops versus flow rates in the passage Z_{C0N1}

The total pressure drop in a passage is the sum of all the pressure drops coming from the serial association of elementary hydraulic resistances. This calculation is illustrated for the passage Z_{C0N1} in Figures 7, 8 and Tables 1, 2.

Figure 9 presents the distribution of total pressures and velocities in the passage Z_{C0PT} obtained from a commercial code (Fluent). The figure shows that the singular losses are predominant, as the flow twists violently at those places. Compared to the singular losses, the frictional ones in tubes can be nearly neglected. The magnitude of the total losses in a passage is in this case mainly associated with the singular losses.

Figure 10 presents several sets of comparative results of CFD and ABM in the main passages of the intermediate block. Both methods introduce approximately the same evolution of the pressure drop as a function of the flow rate. At low Reynolds numbers, the results of the two methods are in good agreement. However, differences between the two methods increase when the Reynolds number increases. Especially for the models made up of a small number of resistance elements, differences become non negligible, as in Figure 10 (a) and (b). These differences arise due to the following reasons:

1. The outlet flow port of the geometry is near to bends or some section change that may have effect on the flow behavior as shown in Figure 10 (a). As a result, the flow is not well developed when it passed through these places. The pressure drop obtained from CFD analysis is thus less than the one calculated from the ABM which assumes decoupled conditions.

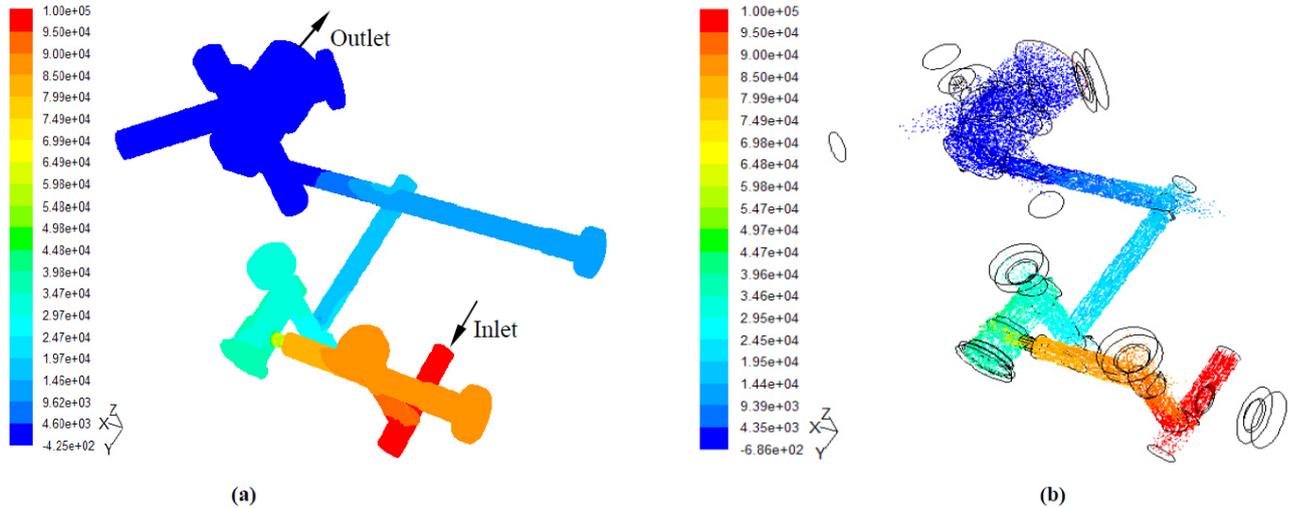


Figure 9. Total pressures profile (a) and velocity evolution (b) of the passage Z_{COPT} in CFD analysis

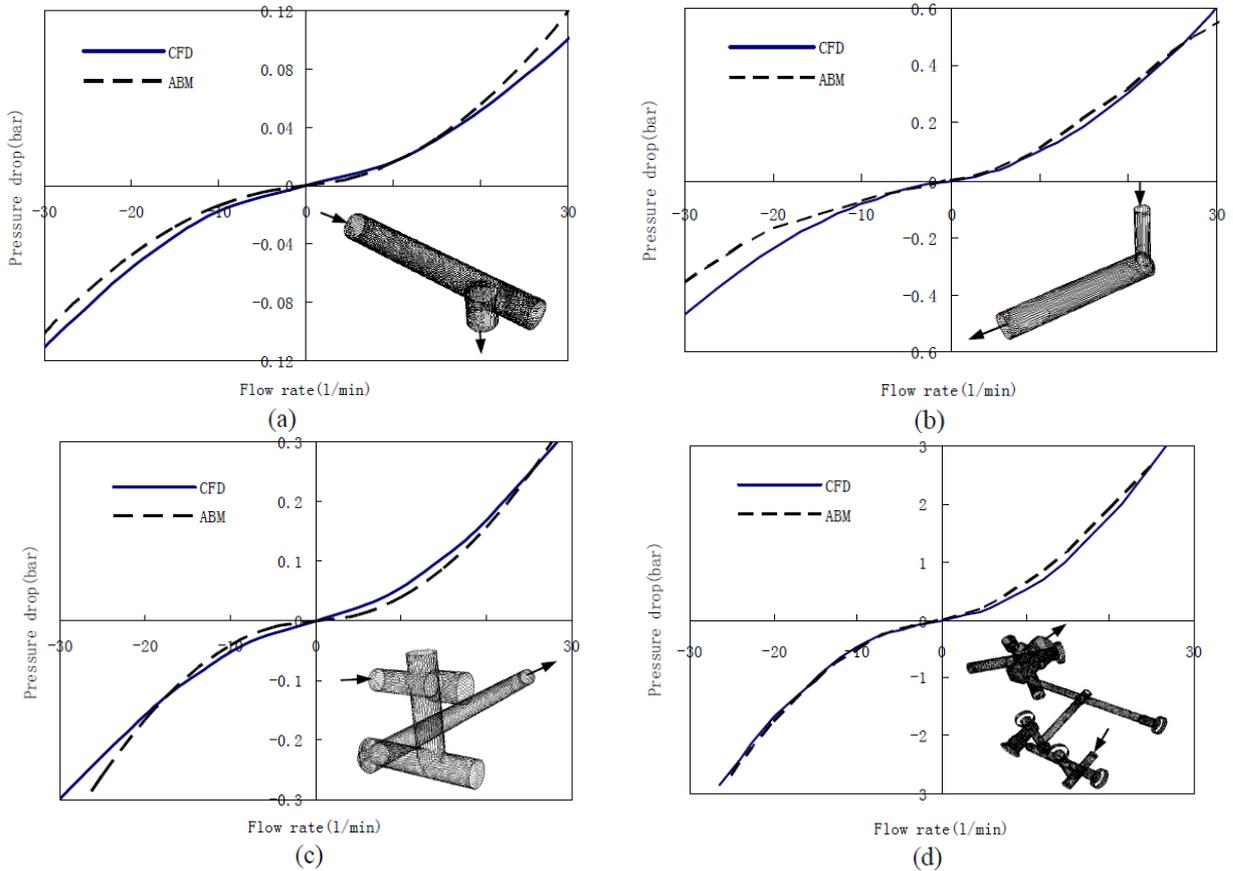


Figure 10. CFD and ABM results of pressure drops with respect to flow rates: (a) Z_{NOVO} ; (b) Z_{BOC0} ; (c) Z_{CONI} ; (d) Z_{COPT}

2. The distribution of the velocity field at inlet port is not properly set. The evolution of the velocity field in the tube can cause additional energy losses.

3. The cases described in the literature do not exactly fit ours. They are used as approximation, which could lead to errors.

4. The accuracy of the CFD analysis depends on the refinement of the model, the calculation method, and the flow regime. To get a more accurate result, we could refine the mesh of the model or implement a turbulent method

when the Reynolds number gets higher. But the computational time is significantly increased.

The two first effects become negligible when the energy dissipation is more important in the middle than at the two ends as in Figure 10 (d).

A set of results of the total energy dissipation in the intermediate block including all the passages between servovalves (A_1 , B_0) towards the actuator chamber volume V_1 in 4-way mode is also shown in Figure 11. In this figure, the pressure drop is calculated between the port B_0 and V_1

with various flow rates at port A_1 . The analytic results coming from ABM involve losses of all related passages and bifurcations. They are in good agreement with the CFD results at low flow rates imposed at port A_1 of servovalve SV21 (Figure 2). Larger differences are observed at high flow rates and can be explained by the stronger influence of the turbulent effects.

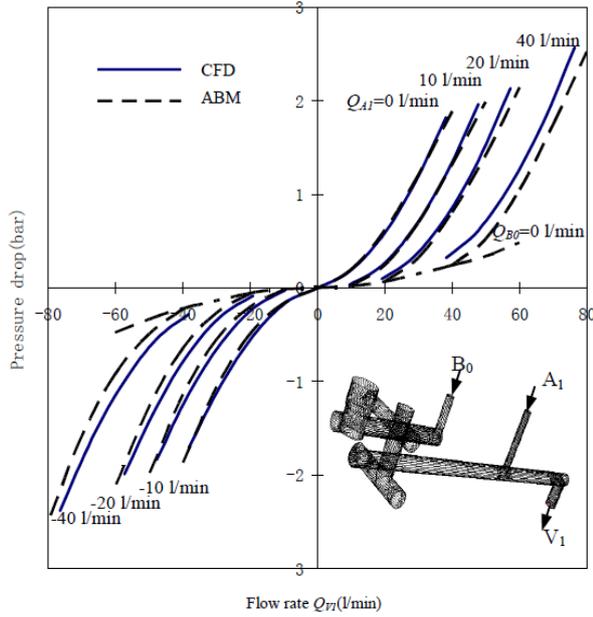


Figure 11. CFD and ABM results of pressure drop between B_0 and V_1 versus flow rates to or from V_1 in a passage from the servovalves to the actuator chamber volume V_1 (4-way mode) with various flow rates at port A_1

4. Compressibility Effect of the Intermediate Block

The volume of fluid in the intermediate block between the servovalve and the actuator induces a compressibility effect. This effect will influence the dynamics of the whole system and decrease the hydraulic pulsation.

If the pressures in each passage are assumed to be identical, the volume effect of the intermediate block can be considered as an additional equivalent volume to each actuator chamber. The additional volume is the sum of the intermediate block volumes joint together. Therefore, although there is no flow in certain passages (Z_{C1N0} and Z_{B1C1}) in mode 1, the additional volumes in modes 1 and 2 are the same as they have the same condition of the passage connection, i.e. the valves V_{20} and V_{21} in ON-position. Table 3 gives the calculated values of the additional volumes for each of the three working modes.

Table 3. Additional volume of each flow path

Working mode	Mode 1	Mode 2	Mode 3
Additional volume 0 (m^3)	$1.0041 \cdot 10^{-4}$	$1.0041 \cdot 10^{-4}$	$7.9754 \cdot 10^{-5}$
Additional volume 1 (m^3)	$1.0041 \cdot 10^{-4}$	$1.0041 \cdot 10^{-4}$	$7.9754 \cdot 10^{-5}$

The additional volumes 0 and 1 correspond to the flow paths from servovalve to the chamber V_0 and V_1 respectively.

Compared to the midstroke actuator volume of $1.56 \cdot 10^{-4} m^3$, the volume in the intermediate block is more than half of it, and hence can not be neglected. This implies that the volume of fluid in the flow path has a significant influence on the system dynamics.

As illustrated in[22], the hydraulic natural frequency of a linear-motion hydraulic actuator can be calculated as follows:

$$f_H = \frac{1}{2\pi} \sqrt{\frac{2B \cdot A^2}{V} \cdot \frac{2}{M}} = \frac{A}{\pi} \sqrt{\frac{B}{MV}} \quad (8)$$

with the hydraulic stiffness:

$$k_H = \frac{2B \cdot A^2}{V} \quad (9)$$

where B is the bulk modulus; A is the active section area of the actuator; M is the mass of the moving part; V is the actuator total volume.

Equations (8) and (9) stand for the case where the actuator is at its midstroke position. For piston at an arbitrary position, the equations should be extended to be:

$$f_H = \frac{1}{2\pi} \sqrt{\frac{k_{H1} + k_{H2}}{M}} \quad (10)$$

where

$$k_{Hi} = \frac{B \cdot A^2}{V_{Ti}} \quad (i=1,2), \quad (11)$$

V_{Ti} is the total equivalent volume of the actuator chamber i .

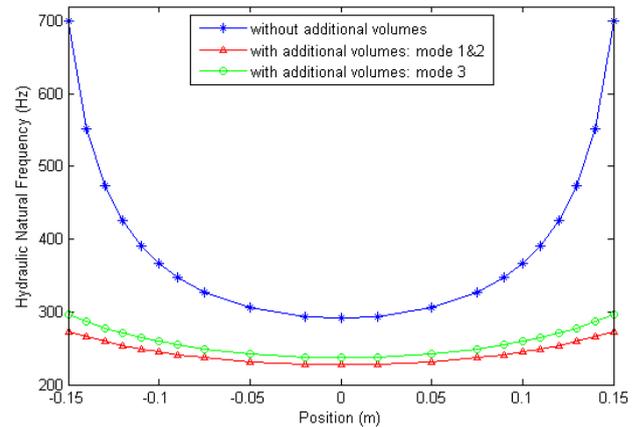


Figure 12. Evolution of the hydraulic natural frequency of the actuator according to piston position with the effect of the intermediate block volumes

Figure 12 presents the evolution of the hydraulic natural frequency of the actuator with respect to the piston position. The result shows that the additional volumes caused by the connection with the intermediate block have an important effect on the evolution of the hydraulic natural frequency. The natural frequency decreases significantly. This frequency at the end of the actuator stroke falls sharply from 700 Hz to 273 Hz for modes 1&2, and to 297 Hz for mode 3.

At midstroke, the natural frequency varies from 292 Hz to 228 Hz (modes 1&2) and to 238 Hz (mode 3).

5. Inertia Effect Study of the Intermediate Block

Although the mass of fluid in the intermediate block is not important, the inertia effect can not be ignored, especially for a high performance system with a large bandwidth. This is mainly due to the small tube section in the intermediate block. The smaller the section is, the larger the velocity of the flow is, and then kinetic energy has to be taken into account.

For ease of implementation of the block inertia effect into the dynamic model and to demonstrate its importance, an equivalent mass of fluid in the block is added to the mass of the moving part of the actuator.

The kinematic energy of the hydraulic system is given by:

$$E = \frac{1}{2}Mv^2 + \frac{1}{2}\rho V_{t1}v_{t1}^2 + \frac{1}{2}\rho V_{t2}v_{t2}^2 + \dots \quad (12)$$

where ρ is the oil density; V_{t1}, V_{t2}, \dots are the oil volume in tube 1, 2, ...; v_{t1}, v_{t2}, \dots are the oil velocity in tube 1, 2, ...

The fluid velocity in the tube i can be calculated as follows:

$$v_{ti} = \lambda_{ti} \cdot \frac{A}{A_{ti}} \cdot v \quad (13)$$

$$\lambda_{ti} = \frac{Q_{ti}}{Q_{total}} \quad (14)$$

where Q_{ti} is the flow rate in the tube i ; Q_{total} is the total flow rate entering into the actuator; A_{ti} is the tube i section area; v is the actuator piston velocity.

Then,

$$E = \frac{1}{2} \left(M + \rho V_{t1} \left(\lambda_{t1} \cdot \frac{A}{A_{t1}} \right)^2 + \rho V_{t2} \left(\lambda_{t2} \cdot \frac{A}{A_{t2}} \right)^2 + \dots \right) v^2 \quad (15)$$

The equivalent mass of the fluid in the tube i is written as:

$$m_{ei} = \rho V_{ti} \left(\lambda_{ti} \cdot \frac{A}{A_{ti}} \right)^2 \quad (16)$$

Table 4 gives the calculated values of the total equivalent mass in each working mode. In this paper, all the calculations are under the assumption that in the mode 2 where two servovalves are used in parallel, the output flow

rates of the servovalves are identical, i.e. λ equals to 0.5 in each branch passage.

Table 4. Fluid Total Equivalent Mass in Each Working Mode

Working mode	Mode 1	Mode 2	Mode 3
Total equivalent mass of fluid (Kg)	4.70	2.80	3.42

The moving part of the actuator has a mass M of 5.8Kg, so that the fluid equivalent mass in Table 4 is very important. This results in an obvious decrease of the hydraulic natural pulsation, similar to the effect of volume in section 4. According to (10) and (11), Figure 13 shows the evolution of the hydraulic natural frequency with consideration both of the volume and inertia effect of the intermediate block. The natural frequency values at the middle and end of stroke are presented in Table 5.

Both volume and inertia effect influence significantly the dynamics of the actuator by decreasing the hydraulic natural frequency. The results show that the volume effect has a more important impact on the natural frequency at the end of the stroke, while the inertia effect gives a proportional decrease all along the stroke.

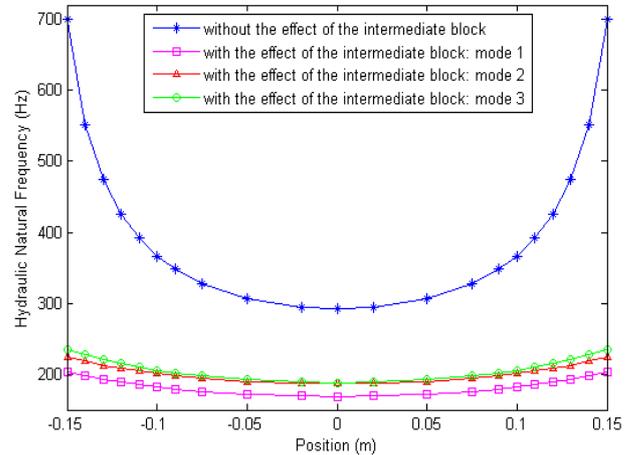


Figure 13. Evolution of the hydraulic natural frequency of the actuator with the effect of the intermediate block

6. Simulation and Experimental Results

Experiments have been conducted on a test bench equipped with a high performance actuator and two large bandwidth servovalves. These hydraulic components are implanted on the intermediate block. The test rig characteristics are presented in Table 6.

Table 5. The Natural Frequency Values (Hz)

Working mode	Mode 1		Mode 2		Mode 3		without the intermediate block	
	Middle	End	Middle	End	Middle	End	Middle	End
with only the volume effect	227.5	273.1	227.5	273.1	237.3	297.1	291.7	700.3
with only the inertia effect	216.8	520.5	239.6	575.1	231.4	555.5	291.7	700.3
with combined effect of the intermediate block	169.1	203.0	186.7	224.3	188.2	235.6	291.7	700.3

Table 6. Test Rig Characteristics

Actuator	
Total stroke	300 mm
Mass of the moving part (rod + piston): M	5.8 Kg
Active section area: A_0	9.456 cm ²
Dead volume at each end	14.184 cm ³
Servovalve Moog D765	
Rated flow	19 l/min
Rated input signal	±10 V
Response time	2 ms
LVDT sensor installed on the rod of the actuator	
Measurement range (MR)	300 mm
Sensibility	4.4 mV/V/mm
Precision	< 0.1% of the MR

All the experimental signals are collected on an analog conditioning unit, and then digitalized at a sampling rate of 1 KHz with 16 bits precision on a dSPACE acquisition board (model DS1104).

Besides, the effect of the intermediate block is also studied by simulation (AMESim). The actuator simulation model takes into account the leakage between the two chambers with a coefficient of $1 \cdot 10^{-4}$ l/min/bar and the viscous friction with a coefficient of 400 N/(m/s). The servovalves are modeled as illustrated in [17]. The temperature of the system and the bulk modulus remain constant during the simulation.

Both experiments and simulations are implemented with a sinusoidal position input of 100 mm amplitude. The system works in mode 2, namely, two servovalves work in parallel to control the actuator. The frequency response results of the simulation and experiment are compared in Figure 14.

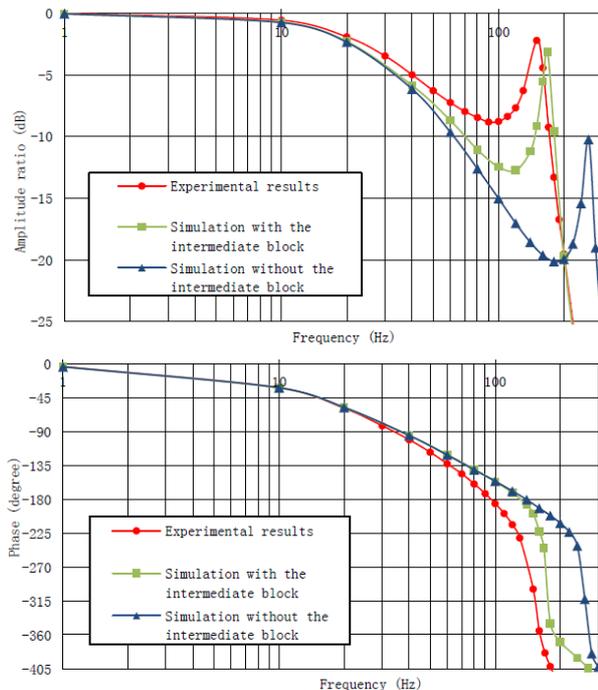


Figure 14. Frequency responses of the system from simulations and experiments in mode 2

The simulation and experimental results show a good agreement at low frequencies. However, differences between

the simulation and experiment become more significant as the frequency grows until 100 Hz. Compared to the simulation results without the intermediate block, the results considering the effect of the intermediate block achieve a better coherence with the experimental ones, particularly for the resonance frequency. The above discussions demonstrate that the effect of the intermediate block takes great importance in the modeling of the hydraulic system, especially at high frequencies. The differences between the simulation and experiment can be explained by the following reasons:

a) Several parameters of the hydraulic system are difficult to obtain, e.g. the bulk modulus, friction coefficient, etc. This may induce some differences between simulation and experimental results;

b) The models used to represent some phenomena may be inefficient in some conditions, for example according to the frequency range. Indeed, dry friction and small servovalve opening can introduce behaviors that change according to the frequency (turbulence, hysteresis);

c) In the calculation of the fluid equivalent mass, the flow rate ratio λ is not strictly constant. It varies with respect to time;

d) The measurement of the sensors contains noise and different types of errors, such as the LVDT phase shift.

7. Conclusions

This paper investigates the modeling of an intermediate block which would probably influence the performance of the hydraulic control system at high frequencies. The model including the compressibility effects, the fluid inertia, and the energy dissipation is developed using Bond Graph approach. Besides, an approach based on abacuses to determine the energy dissipation in each passage has been used and the results have been validated by comparison with CFD analysis. The characteristics of pressure drop versus flow rate were built, and gave the necessary parameters for the lumped parameter model of the intermediate block. Moreover, the compressibility and inertia effects of the intermediate block are studied and the calculated results illustrate that they can cause an obvious decrease in the hydraulic natural frequency. According to the simulation and experiment, we demonstrate that it makes sense to consider the effect of the intermediate block while modeling a hydraulic system with high performance and large bandwidth.

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