

Effect of Vegetation Patch Distribution on the Flow Resistance

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Abstract The presence of aquatic vegetation provides valuable ecosystem services, decreases flow conveyance capacity and generates flow resistance. The resistance due to vegetation depends on flow conditions and vegetation parameters. Few studies have addressed the effect of vegetation distribution on flow resistance. This study investigated the effect of distribution of vegetation patches on the flow resistance and the flow field experimentally in a laboratory flume where rigid cylinders were used to represent vegetation. The vegetation density was kept constant, however, the vegetation was clustered longitudinally and transversally to form different configurations. Results showed that the distribution of vegetation patches was an important parameter in the prediction of flow resistance and the effect of vegetation distribution pattern caused up to 40% extra resistance, while the density of the vegetation remained unchanged. The clustering of vegetation patches along the longitudinal axis of channel generated more friction than did transversal clustering. Evaluation of the effect of distribution pattern of vegetation patches on flow resistance provides valuable information for removing vegetation from streams in a pattern that leads to the maximum reduction in flow resistance.

Keywords Flow resistance, Vegetation, Patch distribution, Clustering

1. Introduction

It is now accepted that the presence of vegetation in aquatic environments serves various purposes, such as the improvement of water quality in wetlands and rivers (Wang et al. 2014; Rowiński et al. 2018, Afzalimehr et al. 2021), coastal protection against storm surges and waves (Möller et al. 2014; Luhar and Nepf 2016), providing a habitat for living organisms and aquatic species, and promoting biodiversity (Yi et al. 2017; Polvi and Sarneel 2018). Aquatic vegetation or macrophytes provide these valuable services through the alteration of flow field (Nepf 2012). Management of aquatic environments and the utilization of aquatic vegetation for the aforementioned services require modelling of the water-vegetation interaction and the underlying physical and biological processes (Marion et al. 2014).

The presence of macrophytes in aquatic environments decreases flow velocity and the conveyance capacity of open channels, as vegetation obstructs the flow and produces hydraulic resistance (Baptist et al. 2010; Green 2005b), consequently the water level rises which may cause flooding of adjacent lands which can be damaging especially in urban

and agricultural areas (Rasmussen et al. 2021). Therefore, attempts are being made to find ways to reduce hydraulic resistance while maintaining the ecological functions of vegetated channels (Luhar and Nepf 2013).

Flow resistance due to vegetation depends on hydraulic and vegetation parameters, such as density, relative submergence, plant morphology, vegetation patchiness, and plant flexibility (Nikora et al. 2008; Fathi-Moghadam et al. 2011; Green 2006). Numerous studies have been done to evaluate the effect of different vegetation parameters on flow resistance (Green 2005a; Nikora et al. 2008; Järvelä 2005, Afzalimehr et al. 2019), but few have addressed the effect of vegetation patch distribution pattern on flow resistance. Literature shows that the effect of vegetation patch distribution on the flow field can have implications for flow resistance (Bal et al. 2011), contaminant removal efficiency (Sabokrouhiyeh et al. 2020), channel morphology, and sediment transport (Shan et al. 2020). Considering that vegetation occurs in heterogeneous patches in the natural environment (Anjum and Tanaka 2019; Schoelynck et al. 2012, Jahadi et al. 2020), this topic calls for a detailed investigation. Furthermore, vegetation is often removed from channels to facilitate flow of water and prevent flooding of adjacent lands (Bal et al. 2017; Errico et al. 2018).

This study experimentally investigates the effect of vegetation patch distribution on the flow field and flow resistance in a laboratory flume using five different

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distribution patterns of vegetation patches. The objectives of this study therefore are to obtain insights into the effect of patchiness on the hydrodynamics of vegetated channels and to determine the pattern of vegetation removal that causes the most reduction of hydraulic resistance.

2. Methodology

Experiments were conducted in a 13 m long and 0.45 m wide horizontal flume located at the Iran Water Research Institution. The water depth was fixed at 24 cm under submerged vegetation condition. 48 Wooden cylinders with a diameter of 1 cm and height of 10 cm were used as vegetation in the flume. Other studies have also used rigid cylinders to represent vegetation (Tinoco, San Juan, and Mullarney 2020). The cylinders were placed together to form different patterns of patches in each experiment (Fig. 1). The number of cylinders for the 5 experiments remained the same so as to keep the density of vegetation constant which was the main parameter effecting flow resistance (Nikora *et al.* 2008; Fathi-Moghadam *et al.* 2011). However, the distribution pattern was changed in order to compare the hydrodynamics of different distribution patterns. The patches were 10 cm apart in the transversal direction and 20 cm apart in the longitudinal direction (except for the last pattern in which the patches were 15 cm apart). The patches were placed at approximately 9 m from the flume entrance to reach the fully developed flow conditions. Gravel with uniform particle size distribution with $d_{50} = 15$ mm was used to cover the bed.

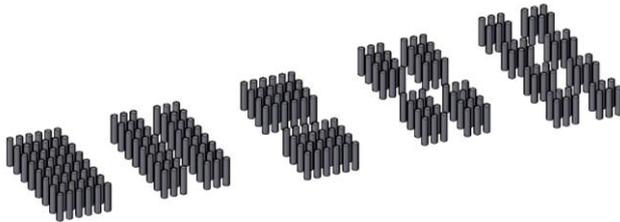


Figure 1. Distribution pattern 1 through 5 from the left

The velocity was measured using a propeller velocimeter which measured the velocity of water in the longitudinal direction of channel. In order to obtain the flow field, the velocity was measured in different cross-sections in the flume (5 cross-sections for the first 2 patterns and 6 for the rest of experiments) with 1 cross-section 10 cm before the leading edge of patches and 2 cross-sections 5 and 20 cm after the trailing edge. Five velocity profiles were measured within each cross-section at 7.5, 15, 22.5, 30 and 37.5 cm from the flume wall in the lateral direction with 8 points measured in the vertical axis in each profile at 3, 4, 5, 7, 10, 15, 20 cm from the bed and 1 point approximately at the water surface. In this study x , y and z are the longitudinal, lateral, and vertical directions, respectively. The flow velocity within the vegetated areas was not measured, since the velocimeter did not work well in this region.

Manning's roughness coefficient was used to quantify the flow resistance (Salah Abd Elmoaty and T. A 2020; Li *et al.* 2014; Miyab *et al.* 2014, Afzalimehr Riazi 2020). After measuring the upstream and downstream velocity, Manning's coefficient was calculated using equations 1 through 3, with V being the velocity, R the hydraulic radius, S the energy slope, l the length of the reach, H_f the friction loss, and h the water depth with u and d subscripts representing the upstream and downstream, respectively,

$$V = \frac{1}{n} R^{\frac{2}{3}} S^{\frac{1}{2}} \quad (1)$$

$$S = \frac{H_f}{l} \quad (2)$$

$$H_f = \left(\frac{V_u^2 - V_d^2}{2g} \right) + (h_u - h_d) \quad (3)$$

Table 1. Hydraulic characteristics of experiments 1 through 5

| | V_u (m/s) | V_d (m/s) | h_u (cm) | h_d (cm) | Fr | n |
|---|-------------|-------------|------------|------------|------|--------|
| 1 | 0.561 | 0.622 | 23 | 21 | 0.4 | 0.0493 |
| 2 | 0.568 | 0.652 | 23 | 20.5 | 0.41 | 0.0523 |
| 3 | 0.562 | 0.659 | 24 | 21 | 0.41 | 0.0582 |
| 4 | 0.566 | 0.647 | 24 | 21 | 0.4 | 0.0598 |
| 5 | 0.547 | 0.625 | 25 | 21.5 | 0.39 | 0.0689 |

The Froude number for the 5 experiments was around 0.4 which has been observed in the field (Mohammadzade *et al.* 2015) and the Reynolds number was around 1.3×10^4 showing the flow was subcritical and turbulent.

3. Results and Discussion

After measuring velocity and flow depth at the upstream and downstream, Manning's coefficient value for the 5 configurations was calculated (presented in table 1). Fig. 2 shows that Manning's coefficient increased as the number of patches (N) increased (almost 40% for the last pattern) with the exception of the second and third configurations which had the same number of patches, however, the third configuration revealed approximately 11% more flow resistance than did the second one. Vegetation was clustered transversally in the second configuration, whereas it was clustered longitudinally in the third pattern.

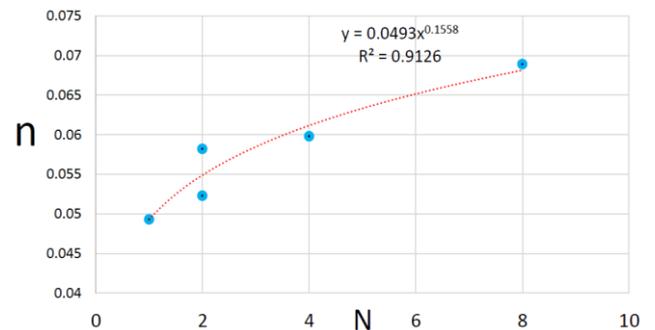


Figure 2. Manning's coefficient (n) against the number of patches (N)

This behavior was reported previously by (Luhar and Nepf 2013) who solved a set of equations developed by using a momentum balance to demonstrate that the flow resistance increased with the increasing number of distinct patches, even though the density of vegetation remained unchanged. Luhar and Nepf (2013) stated that by clustering vegetation into smaller distinct patches, the interfacial area between unobstructed water and vegetation patches increased which caused higher flow resistance. [Why?]

The third configuration led to 11% more resistance than did the second one, even though the second and third patterns both had 2 patches. However, in the second configuration, vegetation was clustered transversally, whereas in the third pattern vegetation was clustered longitudinally. Moreover, the fourth configuration had double the number of patches in comparison to the third, but producing only a little more than 2 % resistance. Noting that the vegetation clustering from the third to the fourth configuration was carried out transversally. Taking these observations into account, it seemed that longitudinal clustering of vegetation caused more hydraulic resistance than did transversal clustering. Figure 3 presents Manning’s n against the number of patches in the longitudinal direction (N). Zhao and Huai (2016) studied the hydrodynamics of discontinuous vegetation patches similar to this study by experimental modelling and large eddy simulations, and stated that flow through vegetation was always non-uniform and the velocity and depth fluctuated as water flowed through vegetation. Discontinuous patches mean more fluctuations which cause more energy loss. However, in this study the velocity and the depth of water were stable without fluctuations when flow passed through patches.

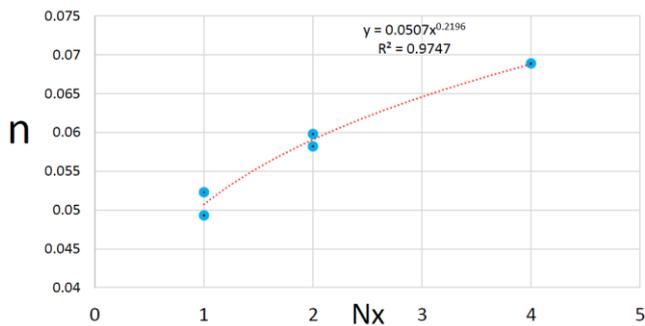


Figure 3. Manning’s coefficient against the number of patches in the longitudinal direction

Bal et al. (2011) investigated the effect of 3 distribution patterns on the flow resistance and concluded that the flow resistance altered significantly when the distribution pattern of vegetation changed and generally the flow resistance increased by clustering patches into smaller patches. In their study, flow resistance increased only for higher discharges when the number of patches increased in the longitudinal direction.

Sabokrouhiyeh et al. (2020) evaluated the effect of

vegetation distribution on the contaminant removal efficiency and concluded that longitudinally clustered vegetation led to more contaminant removal capacity because the flow residence was higher than in the case of elongated patches that were not clustered. Our results showed that longitudinally clustered vegetation produced more hydraulic resistance and that planners and designers must take this into account in addition to ecological and hydraulic considerations.

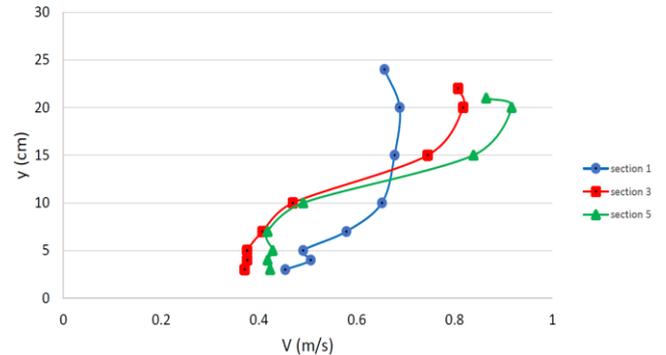


Figure 4. Velocity profile of sections 1, 3 and 5 of the third configuration

Figure 4 shows the velocity profile of the first, third and fifth sections of the third configuration at the center of the flume which was located 10 cm before the leading edge of patches, between the 2 patches and 5 cm after the trailing edge of the second patch, respectively. A secondary peak appears near the bed at $y=4$ cm in the first velocity profile. Comparing the first and third velocity profiles, it is clear that the presence of vegetation had completely altered the flow field, and velocity through the flow field decreased substantially whereas the velocity of the unobstructed field increased as the vegetation retarded the flow and the water was diverted to unobstructed regions of the flume. This alteration of velocity profile is typical of the submerged vegetation condition and has been observed in other studies (Yang, Huai, and Zeng 2020; Chembolu, Kakati, and Dutta 2019; Devi and Kumar 2016; Cui and Neary 2010). Comparing the third and fifth velocity profiles, it was observed that the velocity of the unobstructed region further increased and the depth decreased even more as the water passed through another patch of vegetation. A dip was apparent in the velocity profiles as velocity decreased near the water surface.

Figure 5 shows the velocity contour of section 1 of the fourth configuration in the z-y plane, the contour is plotted from $z=7.5$ to $z=37.5$ cm because a fine grid of measurement needs in the y direction near the walls to achieve a reliable contour, due to considerable variation of velocity in that region. The velocity profile was taken 7.5 cm from both walls. In section 1 located 10 cm behind the patch, the velocity rose rapidly from the bed to approximately $y=10$ cm, showing the thickness of the boundary layer on the top of the gravel bed. In the outer region of this thickness, the velocity variation in the profile was not significant.

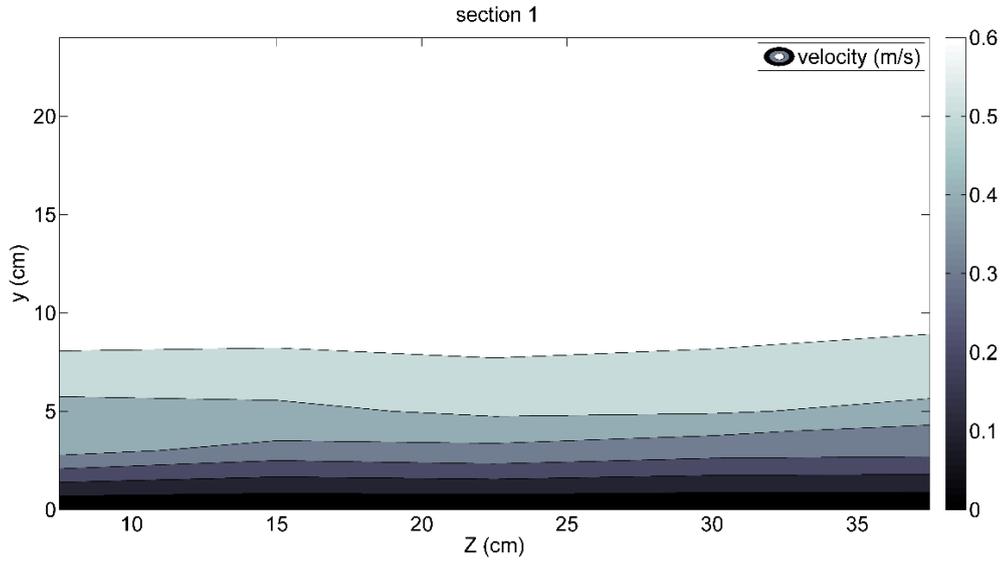


Figure 5. Velocity contour of section 1 of the fourth configuration

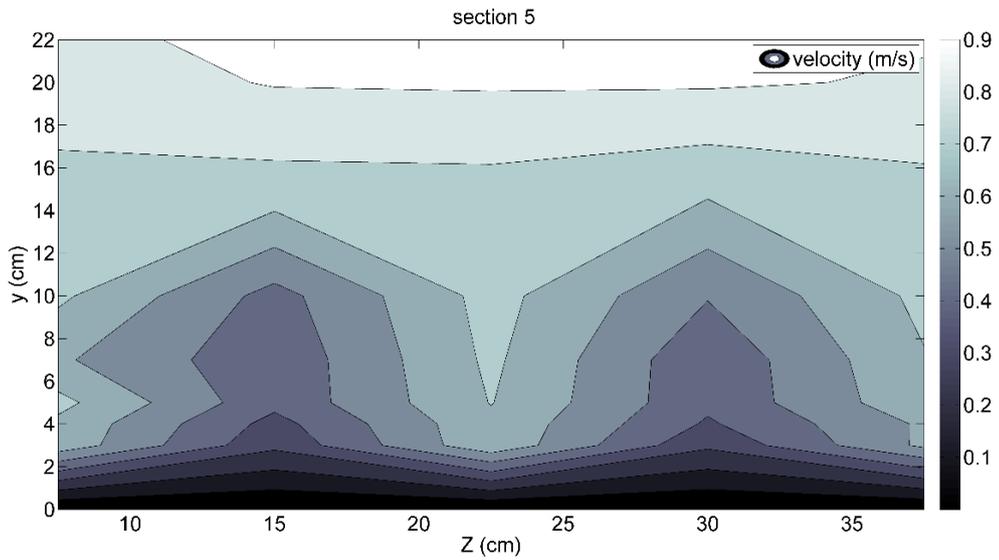


Figure 6. Velocity contour of the section 5 of the fourth configuration

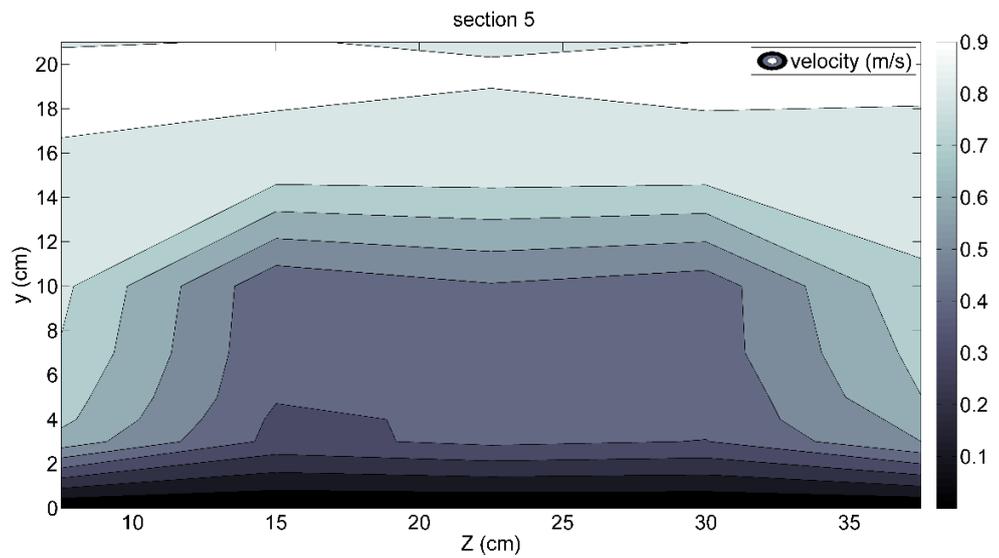


Figure 7. Velocity contour of section 5 of the third configuration

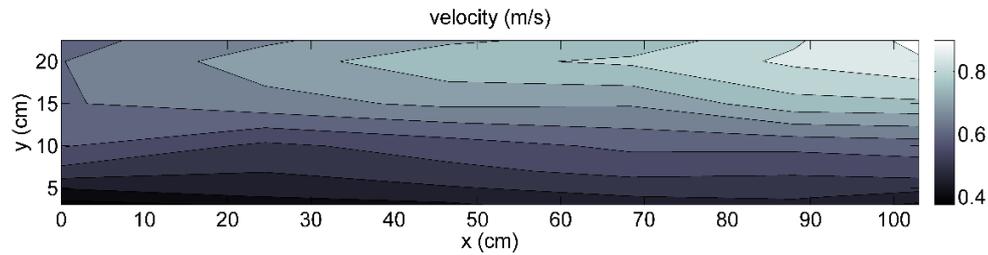


Figure 8. Velocity contour of the fifth configuration in the x-y plane

In section 5 (Fig. 6) located 5 cm after the second row of vegetation, the effect of vegetation on the flow field was obvious, as the velocity reduced from $z=9.5$ cm to $z=17.5$ cm behind the vegetation patch and then increased in the central gap between the patches from $z=17.5$ cm to $z=27.5$ cm and reduced again behind the second patch from $z=27.5$ cm to $z=35.5$ cm in the vertical direction. Accordingly, the velocity rose substantially in the upper regions, reaching 0.9 m/s. In the fourth configuration about 71% of the flow passed through unvegetated region in the flume as the flow was diverted to unobstructed regions. This part of flow was calculated by dividing the z - y plane into 5 areas and multiplying the mean velocity of each profile by the corresponding area.

The section 1 of the third pattern was more or less the same as section 1 of the fourth configuration which was analyzed earlier, the mean velocity and the depth were the same and the velocity contours were nearly identical. However, in section 5 of the third configuration which is presented in figure 7, the flow field was different from that of the fourth configuration, the vegetated area which consisted of a single patch spanned from $z=12.5$ cm to $z=25$ cm in the transversal direction and from the bed to $y=15$ cm in the vertical direction which was discernible, as velocity had dropped significantly in this region. The velocity increased greatly in the upper unobstructed region and reached its maximum value near the surface in a short span as the water was diverted to the unvegetated regions where the depth decreased.

Figure 8 displays the flow non-uniformity through vegetation for the velocity contour of the fifth pattern in the x - y plane. Noting that the velocity profiles were averaged in the z direction, and the flow in the upper unvegetated region rose as the flow passed through the patches in the x axis. However, the velocity changes were insignificant in the lower vegetated region, whereas some studies showed that the velocity and depth variations increased as the water passed through discontinuous patches of submerged vegetation (Ghani et al. 2019; Zhao and Huai 2016). This is because when the velocity increased, the flow depth decreased (25, 24.5, 24, 23, 22 and 21.5 cm in section 1 through 6) monotonically in the x direction.

It is known that water exerts a drag force on the vegetation patch, however, our results confirmed the previous study (Zhao and Huai 2016), that clustering of vegetation in the longitudinal direction produced extra flow resistance and

consequently the drag force of water on vegetation patches increased. Natural vegetation is prone to breaking, dislodgement deflection, and generating more drag on vegetation, showing more hydrodynamic stress on the vegetation (Zhu et al. 2019) which is one of the reasons that vegetation usually grows longitudinally in continuous strips of patches in streams rather than in longitudinally clustered patches which has been observed in other studies (Yamasaki et al. 2019; Zhu et al. 2020).

4. Conclusions

Experiments were carried out to study the effect of vegetation patch distribution on the flow field and flow resistance using rigid cylinders representing vegetation. Results showed that flow resistance varied significantly with the changing vegetation distribution pattern, even though the density remained unchanged which is an important finding because the flow resistance models use density, submergence ratio, and flexibility as input parameters. To our knowledge, no flow resistance model has revealed the effect of different vegetation patch patterns. The longitudinal clustering of vegetation produces more hydraulic resistance than the transversal clustering which has been observed before. Results of this study provide a better restoration approach by considering optimal cutting and removal pattern of vegetation in open channel hydraulics.

REFERENCES

- [1] Afzalimehr, H., Jahadi, M., Zamani, M., and Singh V.P. (2021) Flow structure over bed form with flexible vegetation patches ISH Journal of Hydraulic Engineering, 1-7.
- [2] Jahadi M., Afzalimehr H., Ashrafizadeh M., and Kumar B. (2020). A numerical study on hydraulic resistance in flow with vegetation patch. ISH Journal of Hydraulic Engineering, 1-8.
- [3] Afzalimehr, H., Riazi P., Jahadi, M., and Singh V.P. (2019) Effect of vegetation patches on flow structures and the estimation of friction factor. ISH Journal of Hydraulic Engineering, 1-11.
- [4] Anjum, Naveed, and Norio Tanaka. 2019. 'Hydrodynamics of longitudinally discontinuous, vertically double layered and partially covered rigid vegetation patches in open channel

- flow', *River Research and Applications*, 36: 115-27.
- [5] Bal, K. D., V. Verschoren, J. R. Sara, P. Meire, and J. Schoelynck. 2017. 'Consequences of different cutting regimes on regrowth and nutrient stoichiometry of *Sparganium erectum*.'
- [6] L. and Potamogeton natans.
- [7] L', *River Research and Applications*, 33: 1420-27.
- [8] Bal, Kris, Eric Struyf, Hans Vereecken, Peter Viaene, Liesbet De Doncker, Eric de Deckere, Frank Mostaert, and Patrick Meire. 2011. 'How do macrophyte distribution patterns affect hydraulic resistances?', *Ecological Engineering*, 37: 529-33.
- [9] Baptist, M. J., V. Babovic, J. Rodríguez Uthurburu, M. Keijzer, R. E. Uittenbogaard, A. Mynett, and A. Verwey. 2010. 'On inducing equations for vegetation resistance', *Journal of Hydraulic Research*, 45: 435-50.
- [10] Chembolu, Vinay, Riddick Kakati, and Subashisa Dutta. 2019. 'A laboratory study of flow characteristics in natural heterogeneous vegetation patches under submerged conditions', *Advances in Water Resources*, 133.
- [11] Cui, Jie, and Vincent S. Neary. 2010. 'LES study of turbulent flows with submerged vegetation', *Journal of Hydraulic Research*, 46: 307-16.
- [12] Devi, Thokchom Bebina, and Bimlesh Kumar. 2016. 'Flow characteristics in an alluvial channel covered partially with submerged vegetation', *Ecological Engineering*, 94: 478-92.
- [13] Errico, A., V. Pasquino, M. Maxwald, G. B. Chirico, L. Solari, and F. Preti. 2018. 'The effect of flexible vegetation on flow in drainage channels: Estimation of roughness coefficients at the real scale', *Ecological Engineering*, 120: 411-21.
- [14] Fathi-Moghadam, M., M. Kashefipour, N. Ebrahimi, and S. Emamgholizadeh. 2011. 'Physical and Numerical Modeling of Submerged Vegetation Roughness in Rivers and Flood Plains', *Journal of Hydrologic Engineering*, 16: 858-64.
- [15] Ghani, Usman, Naveed Anjum, Ghufraan Ahmed Pasha, and Muhammad Ahmad. 2019. 'Numerical investigation of the flow characteristics through discontinuous and layered vegetation patches of finite width in an open channel', *Environmental Fluid Mechanics*, 19: 1469-95.
- [16] Green, Julian C. 2005a. 'Comparison of blockage factors in modelling the resistance of channels containing submerged macrophytes', *River Research and Applications*, 21: 671-86.
- [17] Green, Julian C. 2005b. 'Modelling flow resistance in vegetated streams: review and development of new theory', *Hydrological Processes*, 19: 1245-59.
- [18] Green, Julian C. 2006. 'Effect of macrophyte spatial variability on channel resistance', *Advances in Water Resources*, 29: 426-38.
- [19] Järvelä, Juha. 2005. 'Effect of submerged flexible vegetation on flow structure and resistance', *Journal of Hydrology*, 307: 233-41.
- [20] Li, Yiping, Ying Wang, Desmond Ofori Anim, Chunyan Tang, Wei Du, Lixiao Ni, Zhongbo Yu, and Kumud Acharya. 2014. 'Flow characteristics in different densities of submerged flexible vegetation from an open-channel flume study of artificial plants', *Geomorphology*, 204: 314-24.
- [21] Luhar, M., and H. M. Nepf. 2016. 'Wave-induced dynamics of flexible blades', *Journal of Fluids and Structures*, 61: 20-41.
- [22] Luhar, Mitul, and Heidi M. Nepf. 2013. 'From the blade scale to the reach scale: A characterization of aquatic vegetative drag', *Advances in Water Resources*, 51: 305-16.
- [23] Marion, Andrea, Vladimir Nikora, Sara Puijalon, Tjeerd Bouma, Katinka Koll, Francesco Ballio, Simon Tait, Mattia Zaramella, Alexander Sukhodolov, Matthew O'Hare, Geraldene Wharton, Jochen Aberle, Matteo Tregnaghi, Peter Davies, Heidi Nepf, Gary Parker, and Bernhard Statzner. 2014. 'Aquatic interfaces: a hydrodynamic and ecological perspective', *Journal of Hydraulic Research*, 52: 744-58.
- [24] Mohammadzade Miyab N., Afzalimehr H., Singh V. P. and Ghorbani. B. 2014. On Flow Resistance Due to Vegetation in a Gravel-Bed River. *International Journal of Hydraulic Engineering* 3 (3), 8592.
- [25] Mohammadzade Miyab N., Afzalimehr H., and Singh V. P. 2015. *Experimental Investigation of Influence of Vegetation on Flow Turbulence*. Scientific & Academic Publishing.
- [26] Möller, Iris, Matthias Kudella, Franziska Rupprecht, Tom Spencer, Maike Paul, Bregje K. van Wesenbeeck, Guido Wolters, Kai Jensen, Tjeerd J. Bouma, Martin Miranda-Lange, and Stefan Schimmels. 2014. 'Wave attenuation over coastal salt marshes under storm surge conditions', *Nature Geoscience*, 7: 727-31.
- [27] Nepf, Heidi M. 2012. 'Hydrodynamics of vegetated channels', *Journal of Hydraulic Research*, 50: 262-79.
- [28] Nikora, Vladimir, Scott Larned, Nina Nikora, Koustuv Debnath, Glenn Cooper, and Michael Reid. 2008. 'Hydraulic Resistance due to Aquatic Vegetation in Small Streams: Field Study', *Journal of Hydraulic Engineering*, 134: 1326-32.
- [29] Polvi, Lina E., and Judith M. Sarneel. 2018. 'Ecosystem engineers in rivers: An introduction to how and where organisms create positive biogeomorphic feedbacks', *Wiley Interdisciplinary Reviews: Water*, 5.
- [30] Rasmussen, Jes Jessen, Helena Kallestrup, Kirstine Thiemer, Anette Baisner Alnøe, Lisbeth Dalsgaard Henriksen, Søren Erik Larsen, and Annette Baattrup-Pedersen. 2021. 'Effects of different weed cutting methods on physical and hydromorphological conditions in lowland streams', *Knowledge & Management of Aquatic Ecosystems*.
- [31] Rowiński, Paweł M., Kaisa Västilä, Jochen Aberle, Juha Järvelä, and Monika B. Kalinowska. 2018. 'How vegetation can aid in coping with river management challenges: A brief review', *Ecohydrology & Hydrobiology*, 18: 345-54.
- [32] Sabokrouhiyeh, Nima, Andrea Bottacin-Busolin, Matteo Tregnaghi, Heidi Nepf, and Andrea Marion. 2020. 'Variation in contaminant removal efficiency in free-water surface wetlands with heterogeneous vegetation density', *Ecological Engineering*, 143.
- [33] Salah Abd Elmoaty, Mohamed, and El-Samman T. A. 2020. 'Manning roughness coefficient in vegetated open channels', *Water Science*, 34: 124-31.
- [34] Schoelynck, Jonas, Toon de Groote, Kris Bal, Wouter Vandenbruwaene, Patrick Meire, and Stijn Temmerman. 2012. 'Self-organised patchiness and scale-dependent

- bio-geomorphic feedbacks in aquatic river vegetation', *Ecography*, 35: 760-68.
- [35] Shan, Yuqi, Tian Zhao, Chao Liu, and Heidi Nepf. 2020. 'Turbulence and Bed Load Transport in Channels With Randomly Distributed Emergent Patches of Model Vegetation', *Geophysical Research Letters*, 47.
- [36] Tinoco, Rafael O., Jorge E. San Juan, and Julia C. Mullarney. 2020. 'Simplification bias: lessons from laboratory and field experiments on flow through aquatic vegetation', *Earth Surface Processes and Landforms*, 45: 121-43.
- [37] Wang, Chao, Sha-sha Zheng, Pei-fang Wang, and Jin Qian. 2014. 'Effects of vegetations on the removal of contaminants in aquatic environments: A review', *Journal of Hydrodynamics*, 26: 497-511.
- [38] Yamasaki, Taís N., Paulo H. S. de Lima, Diego F. Silva, Cristiane G. de A. Preza, Johannes G. Janzen, and Heidi M. Nepf. 2019. 'From patch to channel scale: The evolution of emergent vegetation in a channel', *Advances in Water Resources*, 129: 131-45.
- [39] Yang, Fan, Wen-Xin Huai, and Yu-Hong Zeng. 2020. 'New dynamic two-layer model for predicting depth-averaged velocity in open channel flows with rigid submerged canopies of different densities', *Advances in Water Resources*, 138.
- [40] Yi, Yujun, Xi Cheng, Zhifeng Yang, Silke Wiecepelt, Shanghong Zhang, and Yingjie Wu. 2017. 'Evaluating the ecological influence of hydraulic projects: A review of aquatic habitat suitability models', *Renewable and Sustainable Energy Reviews*, 68: 748-62.
- [41] Zhao, Fang, and Wenxin Huai. 2016. 'Hydrodynamics of discontinuous rigid submerged vegetation patches in open-channel flow', *Journal of Hydro-environment Research*, 12: 148-60.
- [42] Zhu, J., W. Hu, X. Liu, and J. Deng. 2019. 'A review of the studies on the response of aquatic vegetation to hydrodynamic stress in lakes', *Shengtai Xuebao/ Acta Ecologica Sinica*, 39: 454-59.
- [43] Zhu, Zhengtao, Zhonghua Yang, Wenxin Huai, Huilin Wang, Da Li, and Yujie Fan. 2020. 'Growth-decay model of vegetation based on hydrodynamics and simulation on vegetation evolution in the channel', *Ecological Indicators*, 119.