The KaleidaGraph and the Kontron: "Hands On" Tools in a Physical Chemistry Laboratory for Determination of pK_a of Weak Acids and Weak Bases

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Abstract   A simple and easy laboratory protocol for the determination of the pK_a of a weak acid like hydrazoic acid (HN_3) is described in this paper by measuring the absorbance values of the hydrazoic acid as a function of pH with a 'UVIKON 323 Kontron Instruments' Spectrophotometer. An equation compatible to KaleidaGraph program is derived and used in the program to determine the pK_a. The present protocol for the determination of the pK_a is useful in teaching chemistry experiments in Physical Chemistry Laboratory.

Keywords pK_a, KaleidaGraph, Kontron Instruments, Acid-Base Equilibriums

1. Introduction

The acid-base ionization/dissociation constant, pK_a, is a measure of the tendency of a molecule or ion to keep a proton (H^+) at its ionization center(s), and is related to the ionization ability of the acid or base. pK_a is the core property of an electrolyte that defines chemical and biological behavior. In biological terms, pK_a is important in determining whether a molecule will be taken up by aqueous tissue components or lipid membranes and is related to $\log P$ (where P the partition coefficient). Water is a very polar solvent (dielectric constant $\varepsilon_{20} = 80$), so facile ionization will increase the likelihood of a species to be taken up into aqueous solution. If a molecule does not readily ionize, it will tend to stay in a non-polar solvent such as cyclohexane ($\varepsilon_{20} = 2$) or octanol ($\varepsilon_{20} = 10$). Separation and analytical scientists require an understanding of pK_a because it impacts the choice of techniques used to identify and isolate the compound of interest. pK_a is also closely related to the concept of pH (the acidity of the solution). Hence the knowledge of pK_a values is useful to the majority of the pharmaceutical companies worldwide[1]. Also knowing the acidity constant value (K_a) of an acid and its associated pK_a value is important for medical students for different reasons. The first reason is that the knowledge of pK_a of a drug allows predicting the absorption, bio-reactivity and tissular accumulation as a function of the pH of the medium[2]. Another reason is that the pK_a values of the amino acids of a polypeptide chain are related to the function and structure of the protein[3]. In addition, the pK_a values of different chemical species will help understanding the biological systems[4,5].

2. Experimental

All the chemicals used were of analytical grade. All the solutions were prepared in double distilled water. The absorbance values were recorded on a 'UVIKON 323' Kontron Instruments Spectrophotometer imported from Italy. The software program used for the curve fitting of the absorbance versus pH was a 'KaleidaGraph' from Synergy Software, Reading, PA, USA. The ionic strength was maintained at 1.0 M using KCl. To obtain the absorbance of HN_3 at 250 nm as a function of pH, suitable volumes of HN_3, HCl and KCl are mixed as shown in the table. From each sample 3 mL of solution was taken in 3 mL quartz cuvette and the absorbance was measured. The pH meter used was from 'Radiometer, Copenhagen'.
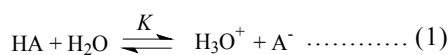
3. Results and Discussion

3.1. Theoretical Basis

The students must be familiar with the acid-base equilibriums. Populations of dissociated and un-dissociated species of weak acid change with pH. Consider the dissociation of a weak acid in aqueous solution

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Table 1. Variation of absorbance of azide (N_3^-)

volume in mL of 0.2 M NaN$_3$ in 1.0 M KCl	volume in mL of 0.2 M HCl in 1.0 M KCl	volume in mL of 1.0 M KCl	pH	Absorbance at 250 nm
1	0.0	19.0	7.209	0.825
1	0.1	18.9	5.416	0.779
1	0.2	18.8	5.050	0.739
1	0.3	18.7	4.802	0.689
1	0.4	18.6	4.614	0.641
1	0.5	18.5	4.421	0.600
1	0.6	18.4	4.212	0.555
1	0.7	18.3	4.031	0.510
1	0.8	18.2	3.814	0.461
1	0.9	18.1	3.548	0.427
1	1.0	18.0	3.134	0.396
1	1.1	17.9	2.897	0.382
1	1.2	17.8	2.638	0.380
1	1.3	17.7	2.467	0.386
1	1.4	17.6	2.357	0.383
1	1.5	17.5	2.271	0.377
1	2.0	17.0	1.981	0.371
1	5.0	14.0	1.395	0.369
1	9.0	10.0	1.109	0.372
1	50 μL	19.0	5.700	0.796
1	25 μL	19.0	6.012	0.803
1	10 μL	19.0	6.417	0.818
1	5 μL	19.0	6.734	0.817
1	0.0	19.0*	8.500	0.825
1	0.0	19.0*	8.012	0.826
1	0.0	19.0*	7.702	0.824
*adjusted with 0.1 M Na$_2$HPO$_4$ and 0.1 M HCl				

$$HA + H_2O \; \underset{}{\overset{K}{\rightleftharpoons}} \; H_3O^+ + A^- \;\cdots\cdots\cdots (1)$$

The equilibrium constant K could be written as

$$K = \frac{[H_3O^+][A^-]}{[HA][H_2O]} \tag{2}$$

or

$$K[H_2O] = \frac{[H_3O^+][A^-]}{[HA]} \tag{3}$$

or

$$K_a = \frac{[H_3O^+][A^-]}{[HA]} \tag{4}$$

Where K_a is the acid dissociation constant, $[H_3O^+]$ is the concentration of hydrogen ion, $[A^-]$ is concentration of salt, and $[HA]$ is that of un-dissociated acid. Taking the logarithms of equation 4, we get

$$\log K_a = \log[H_3O^+] + \log[\text{salt}] - \log[\text{acid}] \tag{5}$$

or

$$pK_a - pH = \log \frac{[\text{acid}]}{[\text{salt}]} \tag{6}$$

Equation 6 contains total of three variables, the pH which is an independent variable and [acid] and [salt] which are two different dependent variables. The two dependent variables must be transformed in to one dependent variable in terms of the absorbance of the species preferably the anion (N_3^-) of the weak acid HN$_3$, so that eventually the equation could best be transformed in to an equation of a locus with two variables. This is done as follows:

Equation 6 is rewritten as

$$(c - x) = \log\left(\frac{a - y}{y - b}\right) \tag{7}$$

Where c is pK_a, x is pH, y is observed absorbance which changes with pH, a and b are the average absorbance of the salt (N_3^-) at highest pH say after the pH between 7.0 and 8.5 and average absorbance of the acid (HN$_3$) at the lowest pH say between 1 and 2 respectively. Therefore (a - y) and (y - b) are the concentrations of the acid and the salt in terms of one variable that is 'y', the absorbance which changes as a function of pH. Therefore equation 7 now contains eventually only two variables x and y. And this could be further transformed in to the equation of a locus with two variables as follows:

Equation 7 could be written as

$$\frac{(a - y)}{(y - b)} = 10^{(c-x)}$$

or

$$(a - y) = (y - b)\, 10^{(c-x)}$$

or

$$a - y = y \bullet 10^{(c-x)} - b \bullet 10^{(c-x)}$$

or

$$y\,(1 + 10^{(c-x)}) = a + b \bullet 10^{(c-x)}$$

or

$$y = \frac{a + b \bullet 10^{(c-x)}}{1 + 10^{(c-x)}} \tag{8}$$

And this is converted to an equation which could be understood by KaleidaGraph software to calculate the pK_a of

HN$_3$ and is written as:

$$y = \frac{(0.825 + 0.372 * 10^{(m1-m0)})}{(1 + 10^{(m1-m0)})} \,;\, m1 = 4.4 \qquad (9)$$

Where m1 = pK_a and m0 = x and 0.825 is 'a' which is the average absorbance above the pH 7 and 0.372 is 'b' which is that of average below the pH 2 and m1 is arbitrarily given a value of 4.4. After several iterations the KaleidaGraph program calculates the pK_a value, which came out to be 4.42 and a locus is passing through the experimental points which is a sigmoid (Figure 1)
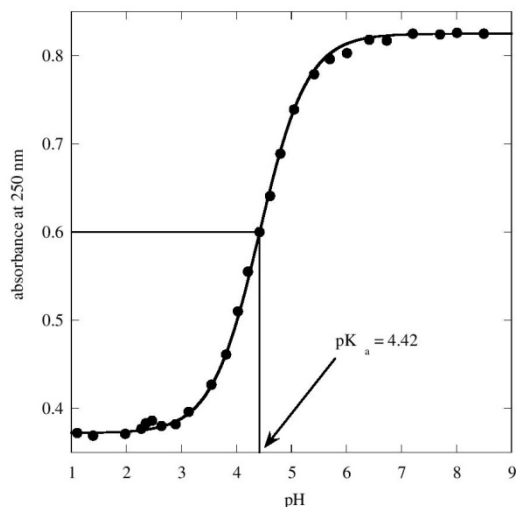

Figure 1.   Plot of absorbance versus pH

In equation 6 the quantity on right hand side is put equal to 1 so that at half neutralization the pH = pK_a. With this condition y comes out to be 0.599 using the values 0.825 and 0.372 for 'a' and 'b' respectively, which is the absorbance of the species at half neutralization. Identifying the value of 0.599 on the y-axis on the graph, proceeding to the locus perpendicularly to the y-axis and from there interpolating on to x-axis gives the pH for half neutralization which is the pK_a of the acid. The literature value of pK_a of HN$_3$ is 4.7[6]. There were several methods of determination pK_a values of weak acids[7].

Hence, the 'KaleidaGraph' software and the Kontron instruments are two 'Hands On' tools for any graduate program laboratory.

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