

Static Characteristics of Two-Axial Groove Journal Bearing Operating on TiO₂ Nanolubricant

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Abstract A modified Krieger-Dougherty viscosity model is used in conjunction with classical two dimensional Reynolds equation to obtain theoretical steady state performance characteristics of two-axial groove journal bearing operating on TiO₂ nano-particle dispersed engine oil. The modified Reynolds equation is non-dimensionalised and solved numerically by finite difference method satisfying the Reynolds boundary condition. A computational code is developed using MATLAB to simulate the bearing characteristics at different eccentricity ratios and volume fractions of TiO₂ nanoparticle additives. Results reveal a significant improvement in load carrying capacity, hydrodynamic pressure distribution, and oil side leakage for two-axial groove journal bearing operating on TiO₂ based nano-oil as compared to plain oil.

Keywords Hydrodynamic journal bearing, Krieger-Dougherty viscosity model, TiO₂ nanoparticles, Reynolds equation, Load carrying capacity, Oil side leakage

1. Introduction

Nanotechnology is poised to bring in revolutionary changes across all spheres of modern life. It is playing an important role in all fields, starting from medicine, manufacturing, defence, and education. Over the last two decades, nano-technology has found a place in tribology with focus on thin film lubrication and also with nanoparticle lubricant additives. Nanoparticles are used as lubricant additives to base oil and these additives play an important role in enhancing the tribological properties of base oil. Considering the scarcity of energy to be prevalent in the days to come, it is necessary to minimise losses due to friction and wear. One of the application of lubricants is in support mechanisms, where journal bearing, being one of the most popular support mechanism used in high load and high speed applications, experiences wear of its surfaces and frictional loss. In the present days nanolubricants are being used in hydrodynamic journal bearings and their application is on the rise.

Over the last few years, many tribologists have been focus-sing on the effect of nanolubricant in hydrodynamic journal bearing. In general, under low loading, the losses due to friction and wear are negligible on contact surfaces. But under heavy loading, the lubricant film generated

between the bearing and journal will be intensely squeezed, and may not be able to protect contact surfaces. Some researches revealed that nanoparticle additives enhance the supporting forces [1]. Therefore, friction and wear can be reduced by adding nanoparticle to the lubricant.

Many studies have been carried out to study the properties of nanolubricant and their application in the past decade. Various types of nanoparticles have been used as lubricant additives and their performance in thin film lubrication have been studied [2-9]. All these studies showed reduced wear and friction in tribo-surfaces with the use of nanoparticle lubricant additives. However, there is a major gap in research regarding theoretical simulation of nanolubricant in fluid film bearing. Available literature suggests improvement in static and dynamic performance characteristics by considering only variable viscosity analysis of nanoparticle additive [10-12]. However viscosity variation with increasing lubricant additive concentration needs to be studied with.

In this study, the influence of lubricant viscosity variation, due to increasing concentrations of nanoparticle additives, on the static characteristics of a journal bearing operating on TiO₂ based lubricant is presented. The viscosity variations has been studied and modelled over the past many decades. Einstein [13] developed the first viscosity model for dilute concentration ($\phi=0.01$) of spherical particles in 1956 and it is expressed in equation-1. Later it was extended by Brinkman [14] and then by Batchelor [15] and it is expressed in equation-2 and equation-3 respectively. In this paper, Modified Krieger-Dougherty

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viscosity model have been employed to predict the relative viscosities of nanolubricant for varying nanoparticle concentrations. The predicted viscosities are then used in the computations of load carrying capacity of two-axial groove journal bearing. The classical Reynolds equation for fluid film lubrication is modified to incorporate relative viscosities of nanoparticle dispersions. The modified equation is solved numerically using finite difference scheme to obtain the pressure profiles for various volume fractions of TiO₂ nanoparticle dispersions. The load carrying capacity is then computed and compared with results for plain oil.

$$\bar{\mu} = \frac{\mu_{ps}}{\mu_{bf}} = 1 + 2.5\phi \quad (1)$$

$$\bar{\mu} = \frac{\mu_{ps}}{\mu_{bf}} = \frac{1}{(1-\phi)^{2.5}} \quad (2)$$

$$\bar{\mu} = \frac{\mu_{ps}}{\mu_{bf}} = 1 + 2.5\phi + 6.5\phi^2 \quad (3)$$

2. Theoretical Analysis

2.1. Governing Equations for Journal Bearing

The governing equation for hydrodynamic journal bearings is the two-dimensional classical Reynolds equation for an incompressible fluid. It is written as:

$$\frac{\partial}{\partial x} \left(h^3 \frac{\partial p}{\partial x} \right) + \frac{\partial}{\partial z} \left(h^3 \frac{\partial p}{\partial z} \right) = 6\mu u \frac{dh}{dx} \quad (4)$$

The solution of the above equation provides the pressure distribution within the oil film developed within the clearance between bearing surface and the journal. Integrating the pressure over the bearing area provides the load carrying capacity of the bearing. Physical configuration of the twin-axial groove journal bearing along with the coordinates is shown in Figure 1.

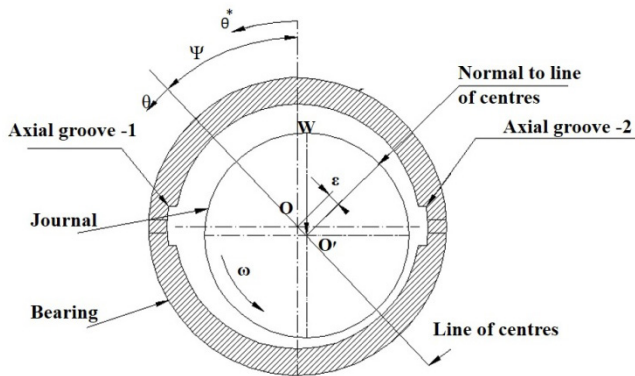


Figure 1. Two-axial groove Journal bearing configuration

In a conventional cylindrical bearing the coordinate θ in

the circumferential direction is taken from the position of maximum film thickness. Here in the grooved bearing, this position needs to be found beforehand. This is done by assuming an arbitrary value of attitude angle ψ and the coordinate θ is measured from the vertical position. Using this ψ , the film thickness for a journal bearing is given by:

$$h = C \left(1 + \varepsilon \cos(\theta^* - \psi) \right) \quad (5)$$

The governing Reynolds equation is non-dimensionalised using the following dimensionless parameters:

$$\text{Angular coordinate: } \theta = \frac{x}{R};$$

$$\text{Axial coordinate: } \bar{z} = \frac{z}{L};$$

$$\text{Bearing length to width ratio:}$$

$$\text{Dimensionless film thickness:}$$

$$\lambda = \frac{L}{D};$$

$$\bar{h} = \frac{h}{C}$$

$$\text{Dimensionless pressure:}$$

$$\bar{p} = \frac{pC^2}{\mu u R};$$

$$\text{Eccentricity ratio: } \varepsilon = \frac{e}{C};$$

$$\text{Non-dimensional relative viscosity: } \bar{\mu} = \frac{\mu_{ps}}{\mu_{bf}}, \text{ Where, } \mu_{ps} \text{ is}$$

the viscosity of nanoparticle suspension in oil and μ_{bf} is the viscosity of base fluid.

The non-dimensional Reynolds equation thus obtained is of the form,

$$\frac{\partial}{\partial \theta} \left[\bar{h}^3 \frac{\partial \bar{p}}{\partial \theta} \right] + \left(\frac{R^2}{L^2} \right) \frac{\partial}{\partial \bar{z}} \left[\bar{h}^3 \frac{\partial \bar{p}}{\partial \bar{z}} \right] = 6\bar{\mu} \frac{\partial \bar{h}}{\partial \theta} \quad (6)$$

Where, the non-dimensional film thickness is expressed as:

$$\bar{h} = \frac{h}{C} = 1 + \varepsilon \cos(\theta^* - \psi) \quad (7)$$

2.2. Solution Methodology

The non-dimensional Reynolds equation, presented as equation-6, is solved numerically using finite difference method.

A rectangular grid is employed and the central difference scheme of discretization is used to numerically formulate the equation. Gauss-Siedel with SOR method is employed for numerical solution. A computer program is developed in MATLAB to calculate all the bearing characteristics at different eccentricity ratio. An illustration of the grid

employed is shown in Figure 2.

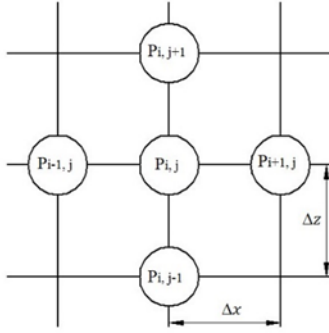


Figure 2. Grid point notation for film extent

In the solution scheme, standard Reynolds boundary conditions are used. The negative pressures arising due to cavitation are neglected. The pressures at the ends of the bearing are also equated to zero, except for groove nodes. The pre-set non-dimensional groove pressure for a finite bearing is provided by Stachowiak [16] as $\bar{p} = 0.2$. The boundary conditions could then be expressed as,

$$\bar{p} = 0.2 \text{ at } \bar{z} = 0 \text{ and } \bar{z} = 1 \text{ at the grooves [16]}$$

$\bar{p} = 0$ at $\bar{z} = 0$ and $\bar{z} = 1$, or all nodes other than nodes in the grooves.

The boundary conditions as applied to the journal bearing are illustrated in Figure 3.

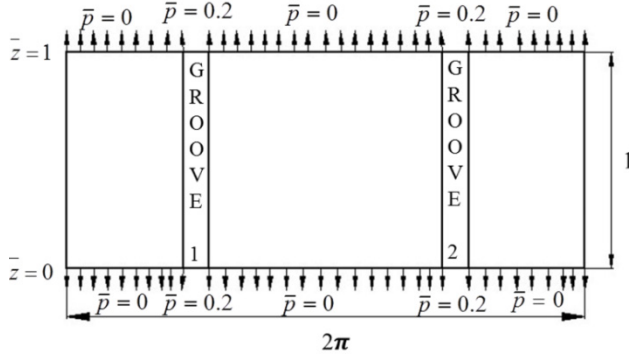


Figure 3. Illustration of Reynolds boundary condition applied to grooved journal bearing

The generated mesh of the bearing area with 130 (circumferential) × 22 (axial) nodes used in the computations is shown in Figure 4. Figure. 4 also shows the node numbers for both the axial grooves.

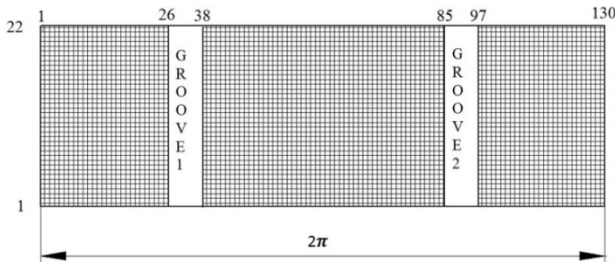


Figure 4. Mesh size and groove nodes

2.3. Nanofluid Viscosity Model

The Krieger–Dougherty equation for shear viscosity of particle dispersions [17] was presented in 1959 covering the full range of particle volume fractions. It was of the form:

$$\bar{\mu} = \frac{\mu_{nf}}{\mu_{bf}} = \left(1 - \frac{\phi}{\phi_m}\right)^{-[\eta]\phi_m} \quad (8)$$

Where ϕ_m is the maximum particle packing fraction, which is approximately 0.605 at high shear rates [18] and η is the intrinsic viscosity, whose typical value for mono disperse suspensions of hard spheres is 2.5 [18, 22]. Equation-8 was later modified by Chen *et al.* [19] to consider the packing fraction within the particle aggregate structure. The modified Krieger–Dougherty equation thus takes the form of equations presented below:

$$\frac{\mu_{nf}}{\mu_{bf}} = \left(1 - \frac{\phi}{0.5} \left(\frac{a_a}{a}\right)^{1.3}\right)^{-1.25} \quad (9)$$

Where, μ_{nf} = Viscosity of nanofluid dispersion,

μ_{bf} = Viscosity of Base oil SAE-30.

Binu *et al* [20] has reported the value of a_a/a for TiO₂ based nanolubricants as 7.77, based on DLS particle size analysis, and used it in modified Krieger–Dougherty viscosity model to study the effects of nanoparticle aggregation on viscosity of nanolubricants and it was validated experimentally with rheological tests. In line with this, the present study also employs the packing fraction a_a/a as 7.77.

The viscosity values are then used in the modified Reynolds equation to obtain the static characteristics.

The non-dimensional modified Reynolds equation for variable viscosity is derived and is presented in the form given below:

$$\frac{\partial}{\partial \theta} \left(\frac{\bar{h}^3}{\bar{\mu}} \frac{\partial \bar{p}}{\partial \theta} \right) + \frac{1}{4\lambda^2} \frac{\partial}{\partial \bar{z}} \left(\frac{\bar{h}^3}{\bar{\mu}} \frac{\partial \bar{p}}{\partial \bar{z}} \right) = 6\bar{u} \frac{d\bar{h}}{d\theta} \quad (10)$$

In the above equation, we define a non-dimensional factor $\bar{\mu} = \mu/\mu_0$. The values of $\bar{\mu}$ is computed in the Matlab code using the modified Krieger–Dougherty model provided in equation-9.

2.4. Steady State Characteristics

2.4.1. Load Carrying Capacity

The load carrying capacity of hydrodynamic journal bearing is obtained by integrating the pressures along the journal surface. Simpson's 1/3 rule is used to perform the integration.

The components of the load along and perpendicular to the line of centres are obtained as follows:

$$\bar{W}_o = \frac{W_o C^2}{\mu U L R^2} = -R \int_0^{2\pi} \int_0^1 \bar{p} \cos(\theta^* - \psi) d\theta d\bar{z} \quad (11)$$

$$\overline{W}_{\frac{\pi}{2}} = \frac{W_{\frac{\pi}{2}} C^2}{\mu U L R^2} = -R \int_0^1 \int_0^{2\pi} \overline{p} \cos(\theta^* - \psi) d\theta d\bar{z} \quad (12)$$

The non-dimensional load carrying capacity is then obtained as:

$$\overline{W} = \sqrt{\overline{W}_o^2 + \overline{W}_{\frac{\pi}{2}}^2} \quad (13)$$

2.4.2. Attitude Angle

The calculation of attitude angle is performed using

$$\phi = \tan^{-1} \left(\frac{\overline{W}_o}{\overline{W}_{\frac{\pi}{2}}} \right) \quad (14)$$

2.4.3. Side Leakage

The total side flow of lubricant is calculated from the formula:

$$Q_z = - \int_0^{2\pi R} \left(\frac{h^3}{12\mu} \frac{\partial p}{\partial x} \right)_{z=L} dx \quad (15)$$

Substituting the non-dimensional parameters gives,

$$Q_z = - \frac{C\omega R^2}{12L} \int_0^{2\pi} \left(\frac{\bar{h}^3}{1} \frac{\partial \bar{p}}{\partial \bar{z}} \right)_{\bar{z}=1} d\theta \quad (16)$$

Therefore, dimensionless lubricant side flow can be written as,

$$\overline{Q}_z = \frac{12LQ_z}{C\omega R^2} \quad (17)$$

The load carrying capacity and oil side leakage are calculated for different volume fractions of TiO₂ and compared with plain engine oil.

3. Results and Discussions

3.1. Validation of Computational Code

Validation of static characteristics of a two axial groove journal bearing has been done in comparison with the standard published values of Pinkus [21]. The MATLAB code generated values are compared with published values of Pinkus [21] and it is given in Table 1.

From Table 1, it can be observed that the computed results from the MATLAB code are in good agreement with the published results of Pinkus [21].

The validated code is used in calculating the hydrodynamic pressures for two-axial groove journal bearings operating on TiO₂ based nanolubricant samples. A sample relative pressure distribution across the bearing area is presented in Figure 5 for TiO₂ nanoparticle concentration and eccentricity ratio.

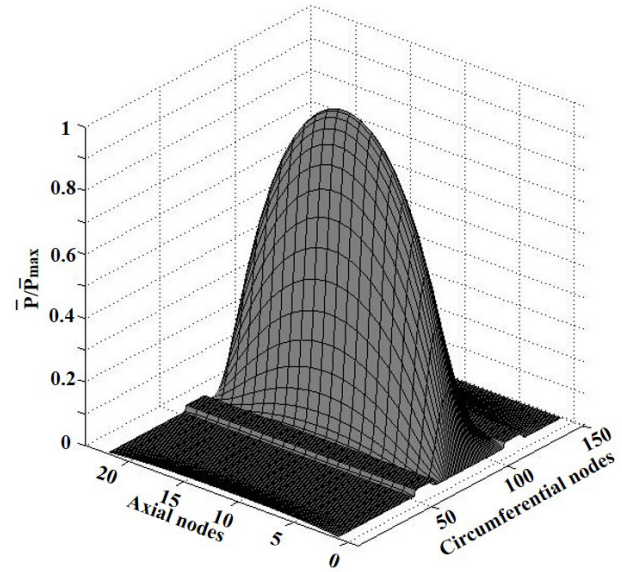


Figure 5. Pressure distribution for $\phi = 0.03$ and $\varepsilon = 0.7$

3.2. Hydrodynamic Pressure Profiles

Figure 6 shows the pressure distribution plot for different additive concentration at the bearing mid-plane. The ratio of non-dimensional pressure to maximum pressure was obtained for an eccentricity ratio of $\varepsilon=0.7$ and additive concentrations ranging from 0.001 to 0.05 volume fraction.

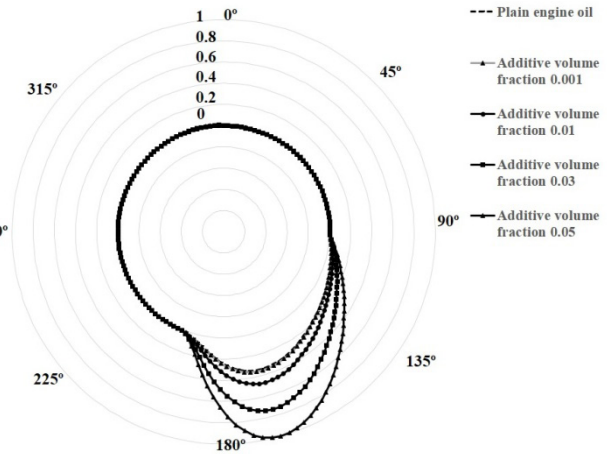


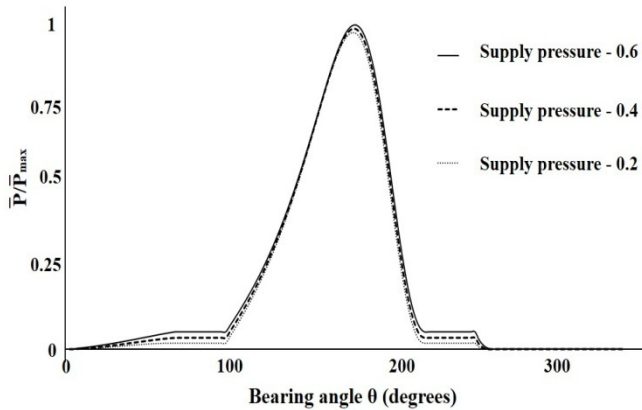
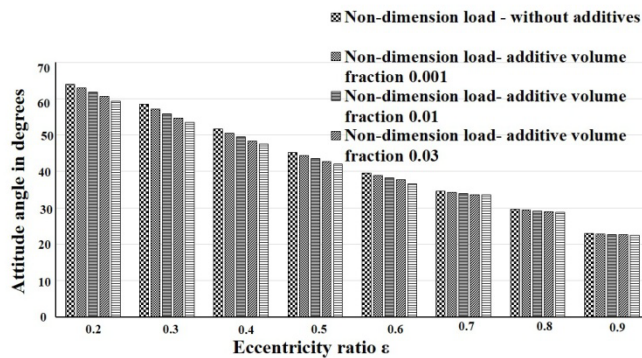
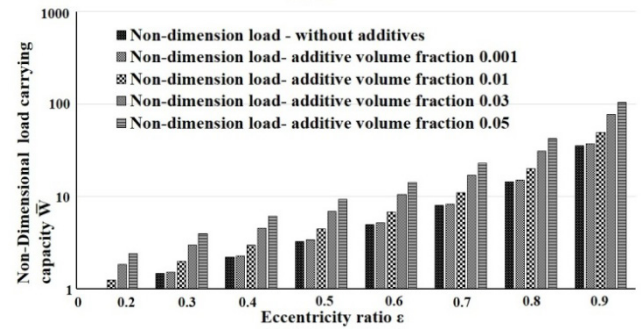
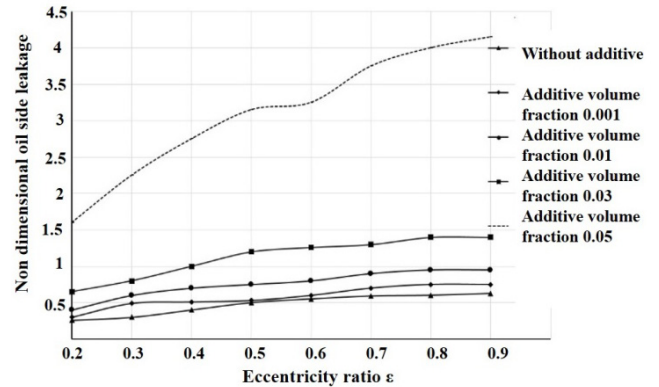
Figure 6. Comparison of non-dimensional pressures for different TiO₂ nanoparticle concentrations at an eccentricity ratio of $\varepsilon=0.7$

It can be observed in Figure 6 that the non-dimensional pressures increase with increasing TiO₂ nanoparticle concentrations. This increase in hydrodynamic pressures could be because of increase in viscosities of corresponding TiO₂ nanolubricant samples. A comparison of non-dimensional pressure for different supply pressure is shown in Figure 7. The increase in supply pressure, a slight increase in hydrodynamic pressure is observed. Figure 8 shows the comparison of attitude angle for different TiO₂ nanoparticle concentrations.

Table 1. Validation of computational code

Eccentricity Ratio	Attitude angle		Flow rate		Sommerfeld Number	
	Pinkus	code	Pinkus	code	Pinkus	code
0.2	64	63.968	0.27	0.3178	0.714	0.6837
0.4	53	51.649	0.43	0.4497	0.275	0.2843
0.6	45	42.588	0.56	0.5446	0.125	0.1302
0.8	28	29.648	0.46	0.6135	0.041	0.0462
0.9	22	22.887	0.43	0.6185	0.019	0.0188

Figure 9 shows the variation of load carrying capacities for different TiO₂ nanoparticle concentrations. It can be observed in Figure 9 that the load carrying capacities increases with increasing TiO₂ nanoparticle concentrations. It is observed that for a very low TiO₂ volume fraction of 0.001, the load carrying capacity is found to increase by only 4%. However, at increasing additive volume fraction of 0.01, the load carrying capacity increases by 40% in comparison to plain engine oil. Figure 10 shows the variation of oil side leakage for different TiO₂ nanoparticle concentrations. It is observed that the oil flow rate increases with increasing TiO₂ nanoparticle concentrations.

**Figure 7.** Comparison of non-dimensional pressures for different supply pressure at an eccentricity ratio of $\epsilon=0.7$ **Figure 8.** Comparison of attitude angle for different TiO₂ nano-particle concentrations and eccentricity ratio**Figure 9.** Comparison of load carrying capacities at different TiO₂ nanoparticle concentrations**Figure 10.** Comparison of Oil side leakage at different TiO₂ nano-particle concentrations

4. Conclusions

The influence of TiO₂ nanoparticle lubricant additives on the static performance characteristics of two-axial groove hydrodynamic journal bearing is theoretically simulated using modified Krieger-Dougherty viscosity model. The study reveals an increase in load carrying capacity of 40%, in comparison to plain engine oil for journal bearings operating on nanolubricant containing TiO₂ nanoparticle additives at a concentration of 0.01 volume fraction. The attitude angle and oil side leakage also shows good results with increasing TiO₂ nanoparticle concentrations. Further experimental studies are however needed to understand better the effect of lubricant additives.

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